

3.5 SINGLE STUB MATCHING USING SMITH CHART:

PROBLEM 1:

A 30m long lossless transmission line with $Z_0 = 50$ ohm operating at 2 MHz is terminated with a load $Z_L = 60+j40$ ohm. If $v=0.6 c$ on the line, find Refection coefficient, the standing wave ratio and the input impedance.

STEP 1:

- To find The normalized load impedance is
- $Z_L' = \frac{Z_L}{Z_0}$
- $Z_L' = \frac{60+j40}{50}$
- $Z_L' = 1.2 +j0.8$

STEP 2:

- Fig 3.5.1, draw the normalized load impedance in smith chart

$$Z_L' = 1.2 +j0.8$$

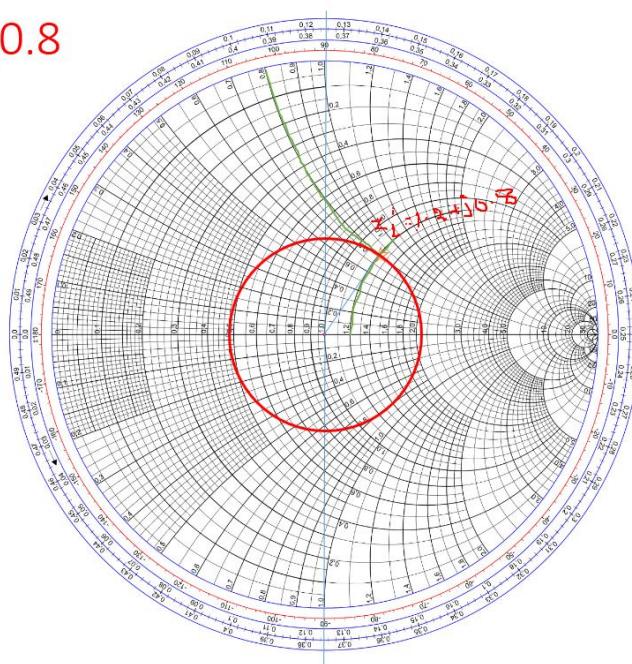


Fig: 3.5.1 Normalized load impedance

STEP 3:

- Fig 3.5.2, mark the value of Standing Wave Ratio in smith chart

$$Z_L' = 1.2 + j0.8$$

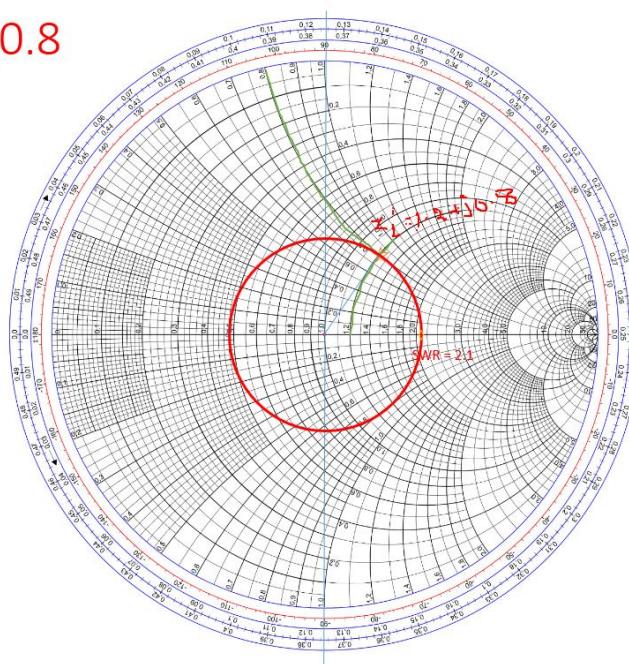


Fig 3.5.2 Standing Wave Ratio

STEP 4:

- Fig 3.5.3, mark the wavelength in smith chart

$$Z_L' = 1.2 + j0.8$$

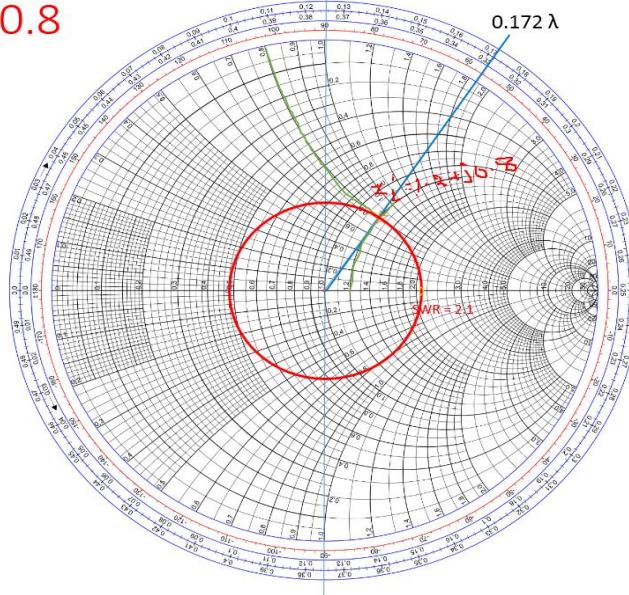


Fig: 3.5.3 wavelength

STEP 5:

- Calculate the velocity and wavelength using 30m long transmission line

$$v = 0.6c$$

$$= 0.6 \times 3 \times 10^8$$

$$= 1.8 \times 10^8$$

$$\lambda = \frac{v}{f}$$

$$\lambda = \frac{1.8 \times 10^8}{2 \times 10^6}$$

$$\lambda = 90 \text{ m}$$

$$L = 30 \text{ m}$$

$$1 \text{ m} = 30 \times \frac{\lambda}{90}$$

$$L = \frac{\lambda}{3}$$

$$L = 0.333 \lambda$$

STEP 6:

- Fig 3.5.4, draw the new wavelength in smith chart



$$z_L' = 1.2 + j0.8$$

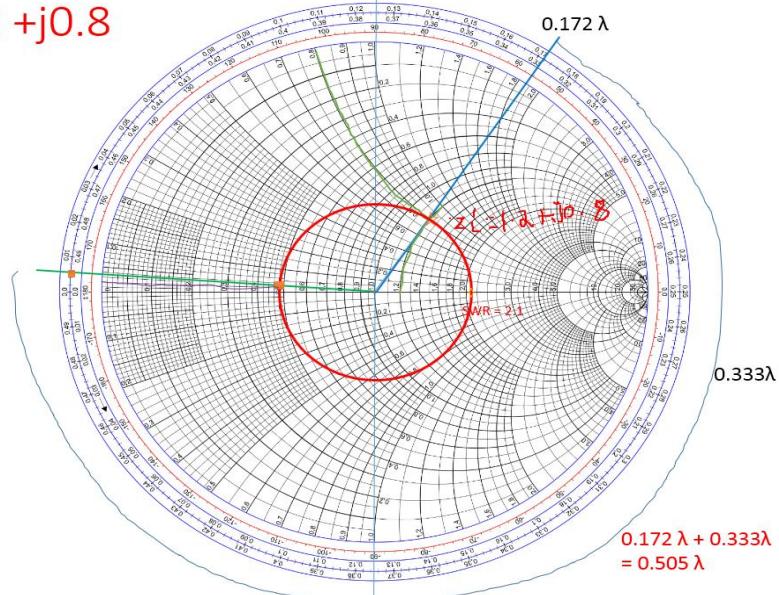


Fig: 3.5.4 new wavelength

STEP 7:

Fig 3.5.5, calculate the normalized input impedance and mark the Z_{in} in smith chart

$$Z_{in} = Z_{in}' Z_0$$

$$Z_{in}' = 0.48 - 0.03$$

$$Z_{in} = (0.48 - j0.03) 50$$

$$Z_{in} = 24 + j1.5 \text{ ohm}$$

 $z_L' = 1.2 + j0.8$

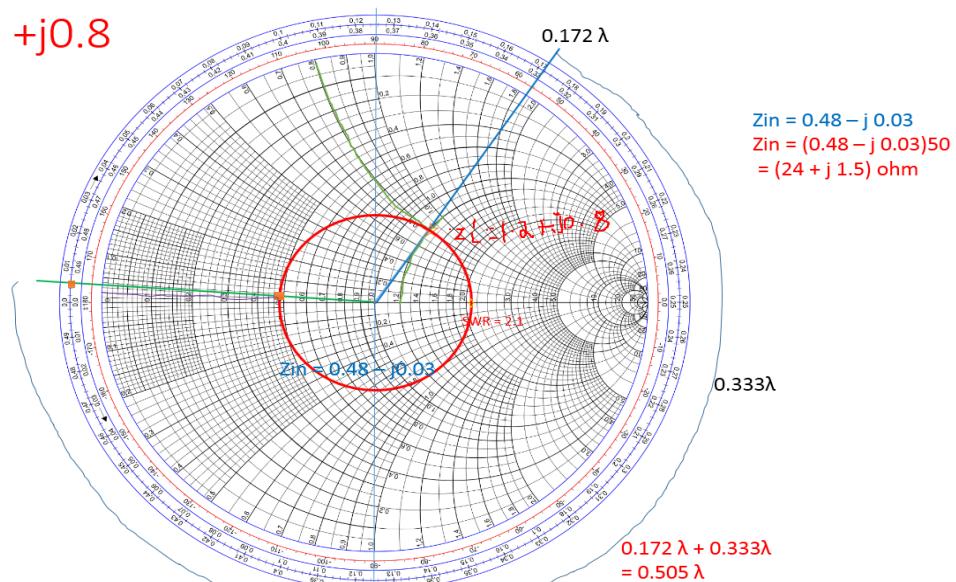


Fig: 3.5.5 Normalized input impedance

STEP 8:

- Fig 3.5.6, mark the reflection coefficient and phase angle in smith chart

 $z_L' = 1.2 + j0.8$

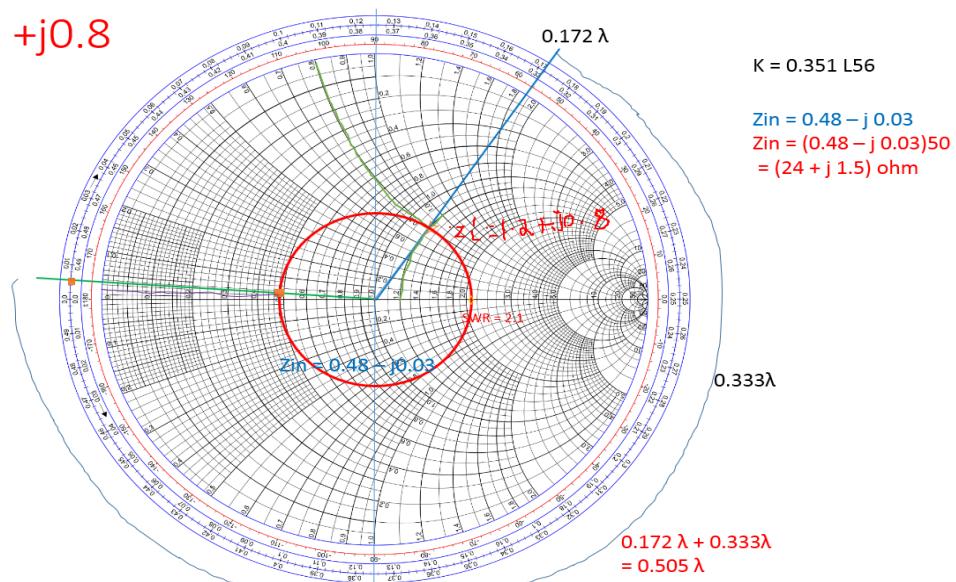


Fig: 3.5.6 Reflection coefficient and phase angle

[Source: John D Ryder, —Networks, lines and fields», 2nd Edition, Prentice Hall India, 2015]

