

## 4.2 Output equation of Induction motor

Output equation is the mathematical expression which gives the relation between the various physical and electrical parameters of the electrical machine.

In an induction motor the output equation can be obtained as follows Consider an 'm' phase machine, with usual notations

Output Q in kW = Input x efficiency

Input to motor =  $mV_{ph} I_{ph} \cos \Phi \times 10^{-3}$  kW

For a 3  $\Phi$  machine  $m = 3$ ,

Input to motor =  $3V_{ph} I_{ph} \cos \Phi \times 10^{-3}$  kW Assuming

$$\begin{aligned} V_{ph} = E_{ph}, V_{ph} = E_{ph} &= 4.44 f \Phi T_{ph} K_w \\ &= 2.22 f \Phi Z_{ph} K_w \end{aligned}$$

$$f = PNs/120 = Pn_s/2,$$

$$\text{Output} = 3 \times 2.22 \times Pn_s/2 \times \Phi Z_{ph} K_w I_{ph} \eta \cos \Phi \times 10^{-3} \text{ kW}$$

$$\text{Output} = 1.11 \times P\Phi \times 3I_{ph} Z_{ph} \times n_s K_w \eta \cos \Phi \times 10^{-3} \text{ kW},$$

$$P\Phi = B_{av}\pi DL, \text{ and } 3I_{ph} Z_{ph}/\pi D = q$$

$$\text{Output to motor} = 1.11 \times B_{av}\pi DL \times \pi Dq \times n_s K_w \eta \cos \Phi \times 10^{-3} \text{ kW}$$

$$Q = (1.11 \pi^2 B_{av} q K_w \eta \cos \Phi \times 10^{-3}) D^2 L n_s \text{ kW}$$

$$Q = (11 B_{av} q K_w \eta \cos \Phi \times 10^{-3}) D^2 L n_s \text{ kW} \text{ Therefore}$$

$$\text{Output } Q = C_o D^2 L n_s \text{ kW}$$

$$\text{where } C_o = (11 B_{av} q K_w \eta \cos \Phi \times 10^{-3})$$

$V_{ph}$  = phase voltage;

$I_{ph}$  = phase current

$Z_{ph}$  = no of conductors/phase

$T_{ph}$  = no of turns/phase

$N_s$  = Synchronous speed in rpm

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$p$  = no of poles,

$q$  = Specific electric loading

$\Phi$  = air gap flux/pole;

$B_{av}$  = Average flux density

$k_w$  = winding factor.

$\eta$  = efficiency

$\cos\Phi$  = power factor

$D$  = Diameter of the stator,

$L$  = Gross core length

$C_o$  = Output coefficient

