



ROHINI

COLLEGE OF ENGINEERING & TECHNOLOGY

Approved by AICTE and Affiliated to Anna University, (An ISO Certified Institution)



ME 8595 THERMAL ENGINEERING II

DEPARTMENT OF
MECHANICAL ENGINEERING

ROHINI COLLEGE OF ENGINEERING AND TECHNOLOGY



DEPARTMENT OF MECHANICAL ENGINEERING

ME8595 - THERMAL ENGINEERING – II

YEAR / SEM: III / V

REGULATION: 2017

LECTURE NOTES

(Both typed and written notes)

Prepared by

MANOJ.J.K

Assistant Professor

ME8595 - THERMAL ENGINEERING - II

UNIT I STEAM NOZZLE

- Types and Shapes of nozzles
- Flow of steam through nozzles
- Critical pressure ratio,
- Variation of mass flow rate with pressure ratio
- Effect of friction
- Metastable flow

UNIT II BOILERS

- Types and comparison
- Mountings and Accessories
- Fuels-Solid, Liquid and Gas
- Performance calculations
- Boiler trial

UNIT III STEAM TURBINES

- Types of steam turbine
- Impulse and reaction principles
- Velocity diagrams
- Work done and efficiency
- Optimal operating conditions
- Multi-staging,
- Compounding
- Governing

UNIT IV COGENERATION AND RESIDUAL HEAT RECOVERY

- Cogeneration Principles
- Cycle Analysis
- Applications
- Source and utilisation of residual heat
- Heat pipes, Heat pumps
- Recuperative and Regenerative heat exchangers
- Economic Aspects

UNIT V REFRIGERATION AND AIR – CONDITIONING

- Vapour compression refrigeration cycle
- Effect of Superheat and Sub-cooling
- Performance calculations
- Working principle of air cycle
- Vapour absorption system
- Thermoelectric refrigeration
- Air conditioning systems
- Concept of RSHF, GSHF and ESHF
- Cooling load calculations
- Cooling towers - concept and types.

TEXT BOOKS

1. Kothandaraman, C.P., Domkundwar .S and Domkundwar A.V., "A course in Thermal Engineering", Dhanpat Rai & Sons, 2016.
2. Mahesh. M. Rathore, "Thermal Engineering", 1st Edition, Tata Mc Graw Hill Publications, 2010.

REFERENCES

1. Arora .C.P., "Refrigeration and Air Conditioning", Tata Mc Graw Hill, 2008
2. Ballaney. P.L ." Thermal Engineering", Khanna publishers, 24th Edition 2012
3. Charles H Butler : Cogeneration" McGraw Hill, 1984.
4. Donald Q. Kern, " Process Heat Transfer", Tata Mc Graw Hill, 2001.
5. Sydney Reiter "Industrial and Commercial Heat Recovery Systems" Van Nostrand Reinholds,1985

CO No.	Course Outcomes	Highest Cognitive Level
17C301.1	Explain the types of nozzles and apply the concept for different velocity flow through a nozzle	K4
17C301.2	Explain the functioning and features of different types of boiler and auxiliaries and calculate performance parameters	K2
17C301.3	Explain the flow in steam turbines, plot velocity diagram and calculate the work done & efficiency	K4
17C301.4	Summarize the concept of cogeneration, working features of heat pump and heat exchangers	K2
17C301.5	Explain the types of Refrigeration & Air-conditioning and its performance	K4

UNIT I

STEAM NOZZLE

- ❖ Types and Shapes of nozzles
- ❖ Flow of steam through nozzles
- ❖ Critical pressure ratio,
- ❖ Variation of mass flow rate with pressure ratio
- ❖ Effect of friction
- ❖ Metastable flow

MANOJ.J.K

AP/MECH

ROHINI CET

- ✓ flow of steam through
- ✓ Critical Pressure ratio
- ✓ Variation of mass flow ratio with Pressure
- ✓ Effect of friction
- ✓ metastable flow

Nozzle:

Nozzle is a device which increases the kinetic energy or velocity and reduces pressure or pressure drops

Steam Nozzle:

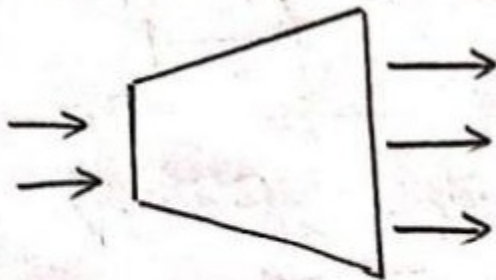
Steam Nozzle is a device which increases the kinetic energy of the steam and reduce pressure of the steam

Types and shapes of nozzle.

- 1 - convergent nozzle

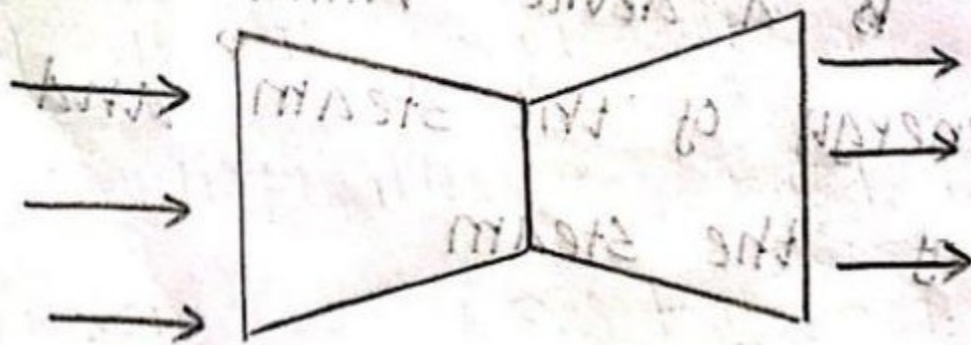
Divergent Nozzle

In Divergent Nozzle the cross sectional area increases from Inlet to Exit:



Convergent Divergent nozzle : [CD nozzle]

In convergent Divergent Nozzle the cross sectional area first decreases from Inlet to throat and then increases from throat to Exit



Flow of steam through Nozzle

The flow of steam through an

The steam entering the nozzle at low velocity and high pressure and leaves at high velocity and low pressure $\rightarrow \rightarrow$

Consider the unit mass of steam ($m = 1 \text{ kg/s}$)

C_1 = Velocity of steam at inlet

C_2 \rightarrow Velocity of steam at Exit

h_1 \rightarrow enthalpy of steam at inlet

h_2 \rightarrow enthalpy of steam at Exit

For steady flow process,

or steady flow energy equation (SFEE)

$$z_1 + \frac{C_1^2}{2} + h_1 + Q = gz_2 + \frac{C_2^2}{2} + h_2 + W$$

Conditions of Nozzle,

$$Q = 0$$

$$W = 0$$

$$z_1 = z_2$$

Apply all the above Conditions in SFEE

$$C_1^2 = C_2^2 + h_2$$

$$C_2 = \sqrt{2(h_1 - h_2) + C_1^2}$$

$C_1 \ll C_2$ so C_1 is negligible ($C_1 \ll C_2$)

$$C_2 =$$

for unit conversion,

$$C_2 = \sqrt{2000(h_1 - h_2)}$$

WKT, $h = C_p T$

$$C_2 = \sqrt{2000 C_p (T_1 - T_2)}$$

Problem 1.1

Dry air at a pressure of 10 bar and

is isentropically expanded to a nozzle

a pressure of 1.2 bar determine

max discharge through the nozzle

$$A = 130 \text{ mm}^2$$

To find:

mass flow, \dot{m}

Solution,

The characteristic gas eqn

$$PV = mRT$$

$$P_1 V_1 = m R T_1$$

For unit mass

$$m = 1 \text{ kg/s}$$

For Air

$$R = 0.287 \text{ kJ/kg K}$$

$$C_p = 1.005 \text{ kJ/kg K}$$

$$\gamma = 1.4$$

From gas equation

$$1000 \times V_1 = 1 \times 0.287 \times 623$$

$$V_1 = 0.178 \text{ m}^3/\text{kg}$$

$$\left(\frac{V_2}{V_1}\right) = \left(\frac{P_1}{P_2}\right)^{1/\gamma}$$

$$V_2 = V_1 \left(\frac{P_1}{P_2}\right)^{1/\gamma}$$

$$V_2 = 0.178 \left(\frac{1000}{120}\right)^{1/1.4}$$

$$V_2 = 0.809$$

$$V_2 = 0.81 \text{ m}^3/\text{kg}$$

For isentropic process,

PT relation,

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}}$$

$$T_2 = T_1 \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}}$$

$$T_2 = 623 \left(\frac{120}{1000}\right)^{\frac{1.4-1}{1.4}}$$

$$m = \rho A C$$

$$m = \rho_2 A_2 C_2$$

$$\rho = m/v$$

$$m = \frac{A_2 C_2}{v_2}$$

$$v = v/m$$

$$v_2$$

$$\rho = 1/v$$

$$= \frac{130 \times 10^{-6} \times 754.2}{0.81}$$

$$0.81$$

$$m = 0.121 \text{ kg/s}$$

Mass of steam discharge through the

For polytropic process,

$$P v^n = C$$

$n = 1.35$ for saturated steam

$n = 1.3$ for super saturated steam

let $P_1 =$ Initial pressure of steam

also reduces

This reduction in enthalpy must be to the increase in kinetic energy, the workdone by the steam is equal the enthalpy drop

$$\text{Workdone, } W = \frac{n}{n-1} (P_1 V_1 - P_2 V_2)$$

Gain in kinetic energy = Workdone during

$$\frac{C_2^2}{2} - \frac{C_1^2}{2} = \frac{n}{n-1} (P_1 V_1 - P_2 V_2)$$

$C_1 \ll C_2$, C_1 is neglected

$$\frac{C_2^2}{2} = \frac{n}{n-1} (P_1 V_1 - P_2 V_2)$$

$$\frac{C_2}{2} = \frac{n}{n-1} P_1 V_1 \left(1 - \frac{P_2 V_2}{P_1 V_1} \right) \quad \text{--- (1)}$$

$$\frac{V_2}{V_1} = \left(\frac{P_1}{P_2}\right)^{1/n} \quad \text{--- 2}$$

Sub eqn (2) in (1)

$$\textcircled{1} \Rightarrow \frac{C_2^2}{2} = \frac{n}{n-1} P_1 V_1 \left[1 - \frac{P_2}{P_1} \left(\frac{V_2}{V_1}\right) \right]$$

$$= \frac{n}{n-1} P_1 V_1 \left[1 - \frac{P_2}{P_1} \left(\frac{P_1}{P_2}\right)^{1/n} \right]$$

$$= \frac{n}{n-1} P_1 V_1 \left[1 - \frac{P_2}{P_1} \left(\frac{P_2}{P_1}\right)^{-1/n} \right]$$

$$= \frac{n}{n-1} P_1 V_1 \left[1 - \left(\frac{P_2}{P_1}\right)^{1 - \frac{1}{n}} \right]$$

$$= \frac{n}{n-1} P_1 V_1 \left[1 - \left(\frac{P_2}{P_1}\right)^{\frac{n-1}{n}} \right]$$

$$\frac{C_2^2}{2} = \frac{n}{n-1} P_1 V_1 \left[1 - \left(\frac{P_2}{P_1}\right)^{\frac{n-1}{n}} \right]$$

$$C_2^2 = 2n P_1 V_1 \left[1 - \left(\frac{P_2}{P_1}\right)^{\frac{n-1}{n}} \right]$$

Sub eqn ③ in above eqn:

$$m_2 \frac{A_2}{V_2}$$

$$m = \frac{A_2}{V_2} \sqrt{\frac{2n}{n-1} P_1 V_1 \left[1 - \left(\frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \right]}$$

From equation 2

$$V_2/V_1 = (P_1/P_2)^{1/n}$$

$$V_2 = V_1 (P_1/P_2)^{1/n}$$

Sub the value of V_2 in m

$$m = \frac{A_2}{V_1 (P_1/P_2)^{1/n}} \sqrt{\frac{2n}{n-1} P_1 V_1 \left[1 - \left(\frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \right]}$$

$$= \frac{A_2}{V_1} \left(\frac{P_2}{P_1} \right)^{1/n} \sqrt{\frac{2n}{n-1} P_1 V_1 \left[1 - \left(\frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \right]}$$

$$m = A_2 \sqrt{\frac{2n}{n-1} \frac{P_1 v_1}{v_1^2} \left[\left(\frac{P_2}{P_1} \right)^{2/n} - \left(\frac{P_2}{P_1} \right)^{\frac{n+1}{n}} \right]}$$

Condition for maximum discharge

$$m = A_2 \sqrt{\frac{2n}{n-1} \frac{P_1}{v_1} \left(\frac{P_2}{P_1} \right)^{2/n} - \left(\frac{P_2}{P_1} \right)^{\frac{n+1}{n}}}$$

There is only one value of the ratio (critical Pressure ratio) $\left(\frac{P_2}{P_1} \right)$, which will produce a maximum discharge

This can be obtained by differentiating mass flow m w.r.t P_2/P_1 and equating it to zero

other quantities except the ratio P_2/P_1 constant

$$\frac{\partial}{\partial (P_2/P_1)} \left[\left(\frac{P_2}{P_1} \right)^{2/n} - \left(\frac{P_2}{P_1} \right)^{\frac{n+1}{n}} \right] = 0$$

$$\left(\frac{P_2}{P_1} \right)^{2/n-1} - \left(\frac{P_2}{P_1} \right)^{\frac{n+1}{n}-1} = 0$$

$$\frac{\binom{P_2/P_1}{2-n}}{\binom{P_2/P_1}{2-n-1}} = \left(\frac{n+1}{2}\right)^n$$

$$\binom{P_2/P_1}{2-n-1} = \left(\frac{n+1}{2}\right)^n$$

$$\binom{P_2/P_1}{1-n} = \left(\frac{n+1}{2}\right)^n$$

$$P_2/P_1 = \left(\frac{n+1}{2}\right)^{\frac{n}{1-n}}$$

$$P_2/P_1 = \left(\frac{2}{n+1}\right)^{\frac{n}{n-1}} \quad \text{--- (7)}$$

(b) $\Rightarrow m = A_2$

$$\sqrt{\frac{2n}{n-1} \left(\frac{P_1}{v_1}\right) \left[\left(\frac{P_2}{P_1}\right)^{2/n} - \left(\frac{P_2}{P_1}\right) \right]}$$

Substitute $n=1.135$ for saturated steam
 and $n=1.3$ for super heated steam.

$m = 0.6356 \times \sqrt{P_1/v_1}$
 $m = 0.6670 \times \sqrt{P_1/v_1}$

2.2062

Case (i)

Put $n=1.135$

$$m_{max} = A \sqrt{\frac{2 \times 1.135}{1.135 - 1} \left(\frac{P_1}{v_1}\right) \left[\left(\frac{2}{1.135 + 1}\right)^{\frac{2}{1.135}} - \left(\frac{2}{1.135 + 1}\right)^{\frac{1.135 + 1}{1.135 - 1}} \right]}$$

0.3799

$$= A \sqrt{5.984 \left(\frac{P_1}{v_1}\right) - 0.3559}$$

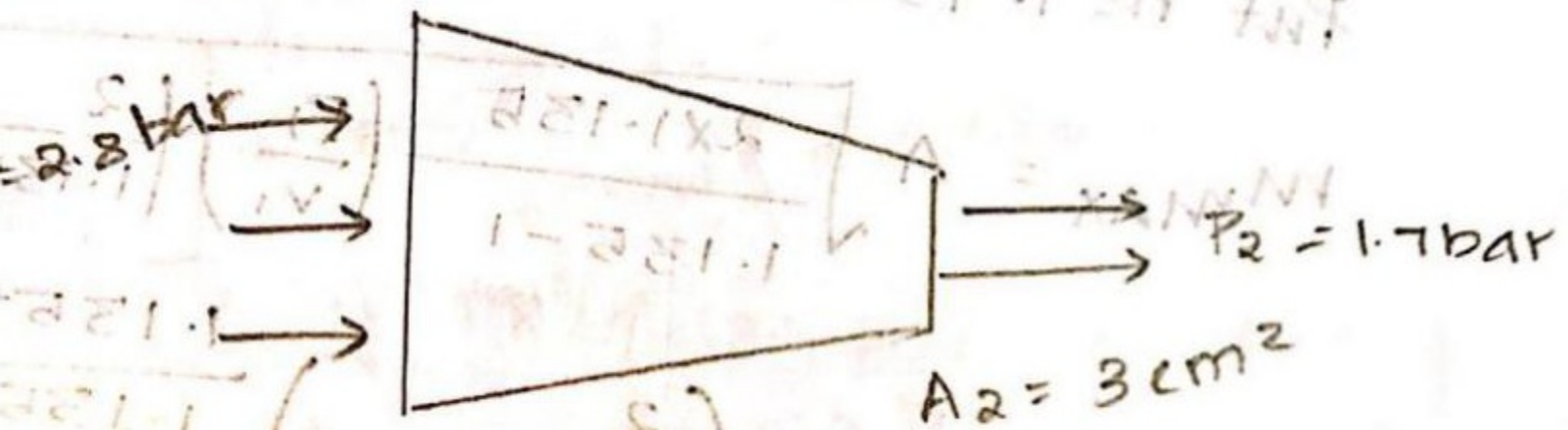
$$= A \sqrt{16.81 \left(\frac{P_1}{v_1}\right) [0.3799 - 0.3799]}$$

$$= A \sqrt{1681 \times 0.024 \left(\frac{P_1}{v_1}\right)}$$

Case (ii) put $n=1.3 = 0.6356$

$$m_{max} = A \sqrt{\frac{2 \times 1.3}{1.3 - 1} \left(\frac{P_1}{v_1}\right) \left[\left(\frac{2}{1.3 + 1}\right)^{\frac{2}{1.3 - 1}} - \left(\frac{2}{1.3 + 1}\right)^{\frac{1.3 + 1}{1.3 - 1}} \right]}$$

exit velocity and mass flow
 for
 (i) isentropic expansion
 (ii) super heated flow



Given:

$$P_1 = 2.8 \text{ bar} = 280 \text{ kN/m}^2$$

$$P_2 = 1.7 \text{ bar} = 170 \text{ kN/m}^2$$

$$A_2 = 3 \text{ cm}^2 = 3 \times 10^{-4} \text{ m}^2$$

find.

C_2 & m for isentropic expansion

For exit condition
from steam tables for $P_2 = 1.07 \text{ bar}$

$$v_{f2} = 0.001056 \text{ m}^3/\text{kg}$$

$$v_{g2} = 1.0309 \text{ m}^3/\text{kg}$$

$$h_{f2} = 483.2 \text{ kJ/kg}$$

$$h_{fg2} = 2215.8 \text{ kJ/kg}$$

$$h_{g2} = 2699.0 \text{ kJ/kg}$$

$$s_{f2} = 1.475 \text{ kJ/kgK}$$

$$s_{fg2} = 5.706 \text{ kJ/kgK}$$

$$s_{g2} = 7.181 \text{ kJ/kgK}$$

WKT, $s_a = s_{f2} + x_2 s_{fg2}$

For expansion the entropy remains const

$$s_1 = s_2$$

$$s_2 = 7.014 \text{ kJ/kgK}$$

$$h_2 = 2632.5 \text{ kJ/kg}$$

To find Exit Velocity

$$C_2 = \sqrt{2000 (h_1 - h_2)}$$
$$= \sqrt{2000 (2721.5 - 2632.5)}$$

$$C_2 = 421.8 \text{ m/s}$$

To find the mass flow rate:-

$$m = \rho_2 A_2 C_2$$

$$m = \frac{A_2 C_2}{\sqrt{2}}$$

$$V_2 = \alpha_2 \sqrt{g_2}$$

$$V_2 = 0.97 \times 1.0309$$

$$V_2 = 1.0 \text{ m}^3/\text{kg}$$

for super heated steam = $n = 1.3$

$$C_2 = \sqrt{\frac{2 \times 1.3}{1.3 - 1} \left(\frac{280 \times 0.646}{2.8 \times 10^5} \right) \left[1 - \left(\frac{280}{170} \right)^{\frac{1.3}{0.646}} \right]}$$

$$C_2 = 412.92 \text{ m/s}$$

To find

From polytropic Pv relation:

$$Pv^n = c$$

$$P_1 v_1^n = P_2 v_2^n$$

$$P_1/P_2 = (v_2/v_1)^n$$

$$v_2/v_1 = (P_1/P_2)^{1/n}$$

$$v_2 = v_1 (P_1/P_2)^{1/n}$$

$$1/1.3$$

$$m = 0.131 \text{ kg/s}$$

ANSWER:

1) Isentropic expansion $C_2 = 421.8 \text{ m/s}$

$$m = 0.126 \text{ kg/s}$$

2) Superheated flow $C_2 = 415.09 \text{ m/s}$

$$m = 0.13 \text{ kg/s}$$

Critical Temperature:

There is only one value of ratio P_2/P_1 which

produces maximum discharge from the

nozzle this ratio is called critical pressure

ratio

where $P_1 =$ Inlet Pressure

$P_2 =$ Exit Pressure

$$P_2/P_1 = \left[\frac{2}{(1.135 + 1)} \right]^{1.135 - 1}$$

$$P_2/P_1 = 0.577$$

Case (ii) for super heated steam $n = 1.3$

$$P_2/P_1 = \left[\frac{2}{1.3 + 1} \right]^{1.3 - 1}$$

$$P_2/P_1 = 0.545$$

Case (iii) for gas $n = 1.4$

$$P_2/P_1 = \left[\frac{2}{1.4 + 1} \right]^{1.4 / 1.4 - 1}$$

steam flow process

Correspond expansion index is 1.135

the ratio of crosssectional Area at and throat for max discharge

Given Data:

$$P_1 = 8 \text{ bar}$$

$$P_2 = 1.5 \text{ bar}$$

$$n = 1.135$$

To find:

$$A_2/A_1 =$$

$$\left[\frac{1 + \frac{n-1}{2} \frac{P_2}{P_1}}{1 + \frac{n-1}{2} \frac{P_1}{P_2}} \right]^{\frac{n}{n-1}}$$

Solution:

Critical Pressure ratio

$$P_c/P_1 = \left[\frac{2}{n+1} \right]^{\frac{n}{n-1}}$$

$$P_t = 4.6 \text{ bar}$$

At inlet Condition (dry)

for steam tables for $P_1 = 8 \text{ bar}$

$$h_1 = 2767.4$$

$$s_1 = s_g = 6.660$$

$$v_1 = s_g = 0.24026$$

At throat condition
from steam tables for

throat pressure

$$P_t = 4.6 \text{ bar}$$

$$v_{f_t} = 0.001090 \text{ m}^3/\text{kg}$$

$$v_{g_t} = 0.40526 \text{ m}^3/\text{kg}$$

$$h_{f_t} = 626.7 \text{ kJ/kg}$$

$$h_{g_t} = 2117.2 \text{ kJ/kg}$$

$$h_{q_t} = 2743.9 \text{ kJ/kg}$$

$$f_{g2} = 467.1 \text{ kJ/kg}$$

$$f_{g2} = 2226.3 \text{ kJ/kg}$$

$$g_{g2} = 2693.4 \text{ kJ/kg}$$

$$s_{g2} = 1.433 \text{ kJ/kg K}$$

$$f_{g2} = 5.790 \text{ kJ/kg K}$$

$$g_{g2} = 7.223 \text{ kJ/kg K}$$

Consider section 1-2

$$s_t = s_f + x_t s_{fgt}$$

or isentropic expansion

$$s_1 = s_t = s_2$$

$$s_t = s_1 = 6.66 \text{ kJ/kg K}$$

$$6.66 = 1.829 + x_t (5.018)$$

$$= \sqrt{2000(267.4 - 265.0)} = 51.1$$

$$C_t = 463.89 \text{ m/s}$$

M.N.T

$$h_f = 3224.51 \text{ kJ/kg}$$

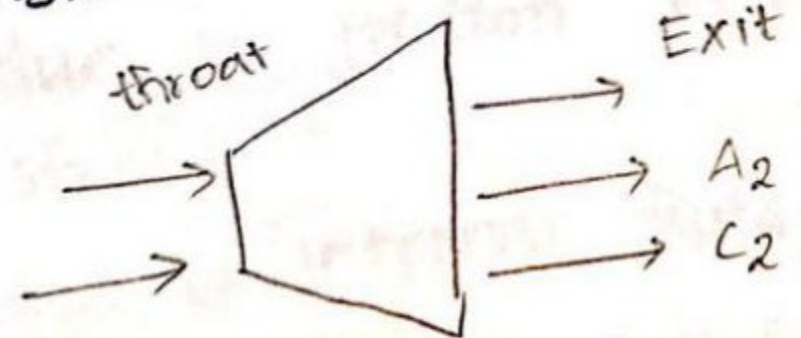
$$V_t = x_f \times V_{gt}$$

$$(\text{at } h_f - h_g) \text{ } \sqrt{2000(3224.51 - 2650)} = 251$$

$$= 0.46 \times 0.40526$$

$$V_t = 0.389 \text{ m}^3/\text{kg}$$

consider section 1-2



$$V_2 = 251 \text{ m/s}$$

M.N.T

$$s_2 = s_{f2} + x_2 s_{fg2}$$

for isentropic expansion $s_1 = s_t = s_2$

$$6.66 \text{ kJ/kg K}$$

$$h_2 = 2470.77 \text{ kJ/kg}$$

K.T

$$h_t = 2659.21 \text{ kJ/kg}$$

$$c_2 = \sqrt{2000 (h_t - h_2)}$$
$$= \sqrt{2000 (2659.21 - 2470.77)}$$

$$c_2 = 613.9 \text{ m/s}$$

$$c_2 = x_2 V_{f2}$$

$$= 0.4 \times 1.159$$

$$V_2 = 1.04 \text{ m}^3/\text{kg}$$

Mass flow rate of steam at throat = mass of flow rate of steam at exit

$$A_2/A_1 = 2.02$$

Effect of friction in a Nozzle

When a steam flows through a Nozzle the final velocity of steam for a given pressure drop is reduced due to the following reasons

- due to friction between nozzle surface and steam
- due to internal fluid friction in steam
- due to shock losses

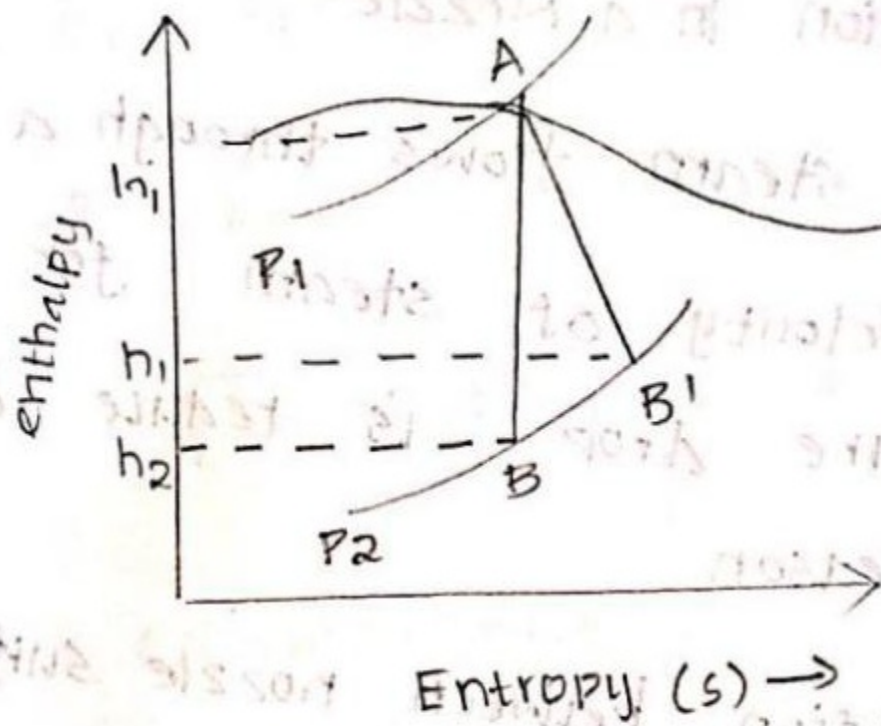
Most of the friction losses occur between the inlet and exit in a convergent-divergent nozzle.

The effect of frictional losses are

- The expansion is no longer isentropic and enthalpy drop is reduced

lower exit velocity

this friction reheating



$h-s$ diagram or Mollier diagram

The enthalpy drop $h_1 - h_2$ is known as

isentropic enthalpy drop. The actual enthalpy drop ($h_1 - h_3$)

Nozzle efficiency or co-efficient of nozzle

It is defined as the ratio of

supplied with
and discharge takes place against
back pressure of 1 bar. The expansion upto
throat is isentropic and the frictional
resistance between the throat and exit
is equivalent to 63 kJ/kg. Take approach
velocity of 75 m/s and throat pressure

- 4 bar. estimate
- 1) Suitable area for the throat to exit
 - 2) over all efficiency of the nozzle
 - 3) based on the enthalpy b/w the
actual inlet pressure and temperature
and the exit pressure

Given:

LD Nozzle

$$m = 2 \text{ kg/s}$$

1 bar

At Exit Condition:

From steam tables for $P_2 = 1 \text{ bar}$

$$V_{f2} = 0.001043 \text{ m}^3/\text{kg}$$

$$V_{g2} = 1.6938 \text{ m}^3/\text{kg}$$

$$h_{f2} = 417.5 \text{ kJ/kg} \quad s_{f2} = 1.303 \text{ kJ/kg}$$

$$h_{fg2} = 2257.9 \text{ kJ/kg} \quad s_{fg2} = 6.057 \text{ kJ/kg}$$

$$h_{gt} = 2675.4 \text{ kJ/kg} \quad s_{g2} = 7.360 \text{ kJ/kg}$$

Consider $1-t$

$$s_t = s_{ft} + x_t \cdot s_{fgt}$$

$$6.78 = 1.776 + x_t \cdot 5.118$$

$$x_t = 0.97$$

At throat the steam is WET

The condition of steam at through is

$$h = h_{ft} + x h_{fgt}$$

$$C_{t2} = \sqrt{2000(h_1 - h_t) + C_1^2}$$

$$= \sqrt{2000(2745 - 2673.6) + 75^2}$$

$$C_t = 498.42 \text{ m/s}$$

At Exit Condition:

$$s_2 = s_f + x_2 (s_{fg2})$$

$$s_2 = s_t = s_1 \text{ (isentropic expansion)}$$

$$6.78 = 1.303 + x_2 (6.057)$$

$$x_2 = 0.90$$

The condition of the steam at exit

$$h_2 = h_{f2} + x_2 h_{fg2}$$

$$h_2 = 417.5 + 0.9 \times 2257.9$$

$$= 2512.61$$

$$\eta_{\text{nozzle}} = \frac{\text{Actual enthalpy drop}}{\text{Isentropic enthalpy drop}}$$

$$= \frac{h_1 - h_2}{h_1 - h_2'}$$

$$= \frac{2795 - 2512.61}{2795 - 2449.61}$$

$$\eta_{\text{nozzle}} = \frac{2795 - 2512.61}{2795 - 2449.61}$$

$$= 81.7$$

To find A_t

$$\dot{m} = \rho A_t C_d V_t$$

$$m = \frac{A_t C_d}{V_t}$$

$$A_t = \frac{m \times V_t}{C_d}$$

$$2512.6 = 417.5 + x_2 (2257.9)$$

$$x_2 = 0.4213$$

$$V_2 = x_2 \sqrt{g_2}$$

$$= 0.42 \times 1.6938$$

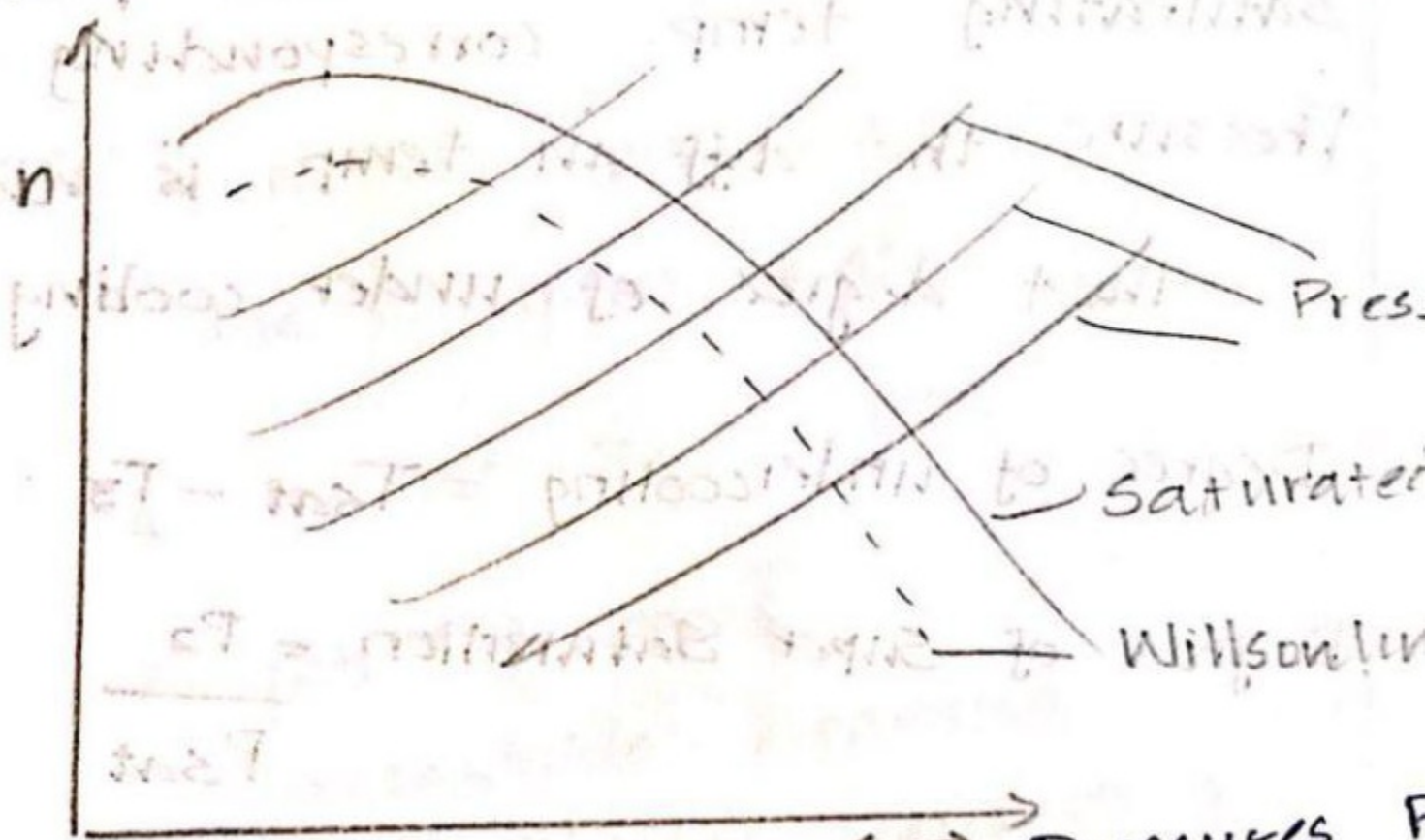
$$V_2 = 155. \text{ m}^3 / \text{kg}$$

$$m = \frac{A_2 C_2}{\sqrt{g_2}}$$

$$2 = \frac{A_2 \times 755.26}{1.55}$$

$$A_2 = 0.00413 \text{ m}^2$$

the condensation rate. so the equal equation
 the expected rate. so the equal equation
 blow liquid and vapour phase is delayed
 and the steam continues to expand
 a dry stage. The steam in such a
 set of condition is set to be super
 saturated or metastable.



The vapour between pressures P
 is said to be super saturated
 and this type of flow in the nozzle
 is known as supersaturated flow

The flow is also called as super cooled flow because at a pressure b/w P_2 and P_3 the temp of the vapour is always lower than saturating temp. corresponding to pressure the diff in temp is known as the degree of under cooling

$$\text{Degree of undercooling} = T_{\text{sat}} - T_2$$

$$\text{Degree of Super Saturation} = \frac{P_2}{P_{\text{sat}}}$$

cross sectional flow area with respect to aspect ratio 3:1. the expansion may be considered as metastable and friction is neglected

2) degree of undercooling and super saturation.

3) loss in available heat drop due to irreversibility

4) Increase in entropy

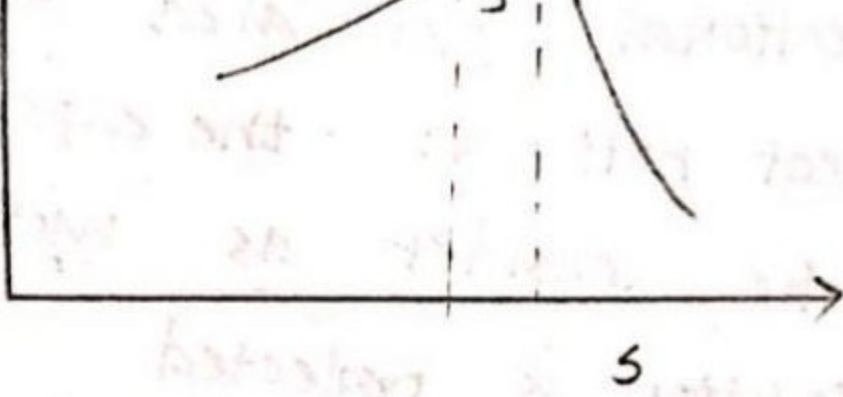
5) ratio of mass flow rate with metastable expansion to that of expansion in thermal equilibrium.

Given:

super heated steam

$$m = 5.2 \text{ kg/s}$$

$$p = 5 \text{ N/m}^2$$



Solution :

At inlet condition :

from steam tables $P_1 = 30 \text{ bar}$, $T_1 = 350^\circ\text{C}$

$$h_1 = 3115 \text{ kJ/kg}$$

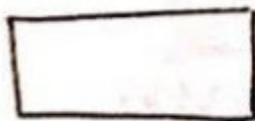
$$s_1 = 6.7 \text{ kJ/kgK}$$

$$v_1 = 0.09 \text{ m}^3/\text{kg}$$

(i) Dimension of the nozzle

Rectangular cross section

Aspect ratio 3:1



for super heated steam $n = 1.3$

$$\frac{c_2}{2} = \frac{n}{n-1} P_1 V_1 \left[1 - \left(\frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \right]$$

$$gz_1 + \frac{c_1^2}{2} + h_1 + Q = gz_2 + \frac{c_2^2}{2} + h_2 + Q_w$$

$$h_1 - h_2 = \frac{c_2^2}{2} - \frac{c_1^2}{2}$$

$$c_2 = \sqrt{2000 (h_1 - h_2)}$$

$$c_2 = 432.7 \text{ m/s}$$

$$P_1 V_1^n = P_2 V_2^n$$

$$V_2 / V_1 = (P_1 / P_2)^{1/n}$$

$$V_2 = V_1 (P_1 / P_2)^{1/n}$$

$$= 0.09 (30/4)^{1/1.3}$$

$$V_2 = 0.424 \text{ m}^3/\text{kg}$$

$$A_2 = 1 \times 1$$
$$= 3x \times x$$

$$A_2 = 3x^2$$

$$\text{Total Nozzle} = 6$$

$$A_2 = 6 \times 3x^2$$

$$A_2 = 18x^2$$

$$0.00286 = 18x^2$$

$$x = 0.0114 \text{ m}$$

$$\text{length } l = 3x = 3 \times 0.0114$$

$$l = 0.0343 \text{ m}$$

$$\text{length of the Nozzle} = 0.0345 \text{ m}$$

$$\text{width of the Nozzle} = 0.0114 \text{ m}$$

Degree of under cooling (and) Super saturation

$$\text{Degree of undercooling} = T_{\text{sat}} - T_2$$

$$T_2 = 391.3 \text{ K} = 118.3 \text{ }^\circ\text{C}$$

from steam table saturation temp at 4

$$T_{\text{sat}} = 143.6 \text{ }^\circ\text{C}$$

$$\begin{aligned} \text{Degree of undercooling} &= T_{\text{sat}} - T_2 \\ &= 143.6 - 118.3 \\ &= \underline{25.27} \text{ }^\circ\text{C} \end{aligned}$$

$$\text{Degree of super saturation} = \frac{P_2}{P_{\text{sat}}}$$

from steam table for saturation pressure

$$T_2 = 118.3 \text{ }^\circ\text{C}$$

$$P_{\text{sat}} = 1.863 \text{ bar}$$

$$\text{Degree of super saturation} = \frac{4}{1.863}$$

$$= 2.14$$

$$\text{Degree of undercooling} = \underline{118.3} \text{ }^\circ\text{C}$$