

Beam Column

4.3 Design a Beam column

Example 3

A beam column is to be designed to support a factored axial load of 500KN(tension). Factored moments M_x acting at top and bottom of the column are 30KNm and 50KNm respectively. Effective length of the column may be taken as 3.2m. Assuming $f_y = 250\text{N/mm}^2$, Design the beam column section and check the same to conform to the specifications of the Indian standard code IS 800 - 2007

Given data

Factored axial load 'P' = 600 KN

Bending moment at top = 30KNm

Bending moment at bottom = 50KNm

Effective length 'fy' = 3.2m

Step 1 : Selection of beam column section

Assuming the same ISHB 250 rolled steel section

Sp 6(1) 1964 page. No. 4, code book

A = 64.96cm²

= 6496mm²

h = 250mm

B = 250mm

Tf = 9.7mm

Ry = rmin

= 5.49cm

= 54.9mm

$$T_w = 6.9\text{mm}$$

Slenderness ratio

$$\begin{aligned} KL/r_{\min} &= 1 \times 3200 / 54.9 \\ &= 58.3 \end{aligned}$$

$$\begin{aligned} P_e &= P + 2M_{\text{bot}} / h \\ &= 600 + 2 \times 50 / 0.25 \\ &= 800\text{KN} \end{aligned}$$

Compressive stress

IS 800 - 2007 page. No. 42, code book

$$f_{cd} = 170 \text{ N/mm}^2$$

Design strength of beam column

$$\begin{aligned} &= f_{cd} \times A / 1000 \\ &= 170 \times 6496 / 1000 \\ &= 1104 \text{ KN} > 800\text{KN} \end{aligned}$$

Hence the selected section is safe

Step 2 : Section properties

$$\begin{aligned} I_{xx} &= 7736\text{cm}^4 \\ &= 7736 \times 10^4\text{mm}^4 \end{aligned}$$

$$\begin{aligned} I_{yy} &= 1961\text{cm}^4 \\ &= 1961 \times 10^4\text{mm}^4 \end{aligned}$$

$$\begin{aligned} R_x &= 10.9\text{cm} \\ &= 109\text{mm} \end{aligned}$$

$$Z_x = 618.9\text{cm}^3$$

$$= 618.9 \times 10^3 \text{ mm}^3$$

$$Z_y = 156.9 \text{ cm}^3$$

$$= 156.9 \times 10^3 \text{ mm}^3$$

$$R_1 = 10 \text{ mm}$$

Check the section

IS 800 - 2007 page. No. 18, code book

$$b/t_f = 250/9.7$$

$$= 25$$

This section is semi compact

Moment

IS 800 - 2007 page. No. 30, code book

$$M_{dx} = Z_x \times f_y / \gamma_{mo}$$

$$= 618.9 \times 10^3 \times 250 / 1.1$$

$$= 140.7 \times 10^6 \text{ Nmm}$$

$$= 140.7 \text{ KNm}$$

(a) Design shear strength due to yielding

IS 800 - 2007 page. No. 32, code book

$$T_{dg} = f_y \times A_g / \gamma_{mo}$$

$$= 250 \times 6496 / 1.1$$

$$= 1476.3 \times 10^3 \text{ N}$$

$$= 1476.3 \text{ KN}$$

(b) Design shear strength due to rupture

$$T_{dn} = 0.9 \times f_u \times A_n / \gamma_{m1}$$

$$= 0.9 \times 410 \times 6496 / 1.25$$

$$= 1916 \times 10^3 \text{ N}$$

$$= 1916 \text{ KN}$$

Take least value

The design strength $T_d = 1476.3 \text{ KN}$

Step 3 : Check for resistance of cross section to combined effects

IS 800 - 2007 page. No. 70, code book

$$[N / N_d + M_x / M_{dx} + M_y / M_{dy}] < 1$$

$$N_d = A_g \times f_y / \gamma_{m0}$$

$$= 6496 \times 250 / 1.1$$

$$= 1476.3 \times 10^3$$

$$= 1476.3 \text{ KN}$$

$$M_x = 50 \text{ KNm}$$

$$M_{dx} = 140.7 \text{ KNm}$$

$$[N / N_d + M_x / M_{dx}]$$

$$= 600/1476.3 + 50/ 140.7$$

$$= 0.756 <$$

Hence safe

Step 4 : Check for resistance of cross section to combined effects

$$M_{eff} = [M - \psi \times T \times Z_e / A]$$

$$= 50 \times 10^6 - 0.8 \times 600 \times 10^3 \times 618.9 \times 10^3 /$$

$$6496$$

$$= 4.3 \text{ KNm} < 140$$

Hence safe

Step 5 : Check for overall buckling strength

$$\begin{aligned} & [P / P_{dx} + M_{eff} / M_{dx}] \\ & = 600/1476.3 + 4.3/ 140.7 \\ & = 0.433 < 1 \end{aligned}$$

Hence safe

Example 4

A beam column is to be designed to support a factored axial load of 500KN (tension). Factored moment M_x Acting at top and bottom of the column are 30 KNm and 50KNm respectively. Effective length of column may be Taken as 3.2m. Assuming $f_y=250\text{N/mm}^2$, design the beam column section and check the same to conform the Specification of the Indian standard code IS 800:2007.

Solution:

Given data:

$$\text{Factored axial load} = 600\text{KN (tension)}$$

$$\text{Bending moment at top} = 30\text{KNm}$$

$$\text{Bending moment at bottom} = 50\text{KNm}$$

$$\text{Yield stress of steel} = 250\text{N/mm}^2$$

Step 1 Selection of beam column section

$$\begin{aligned} M_{dx} & = Z_0 f_y / \gamma_{mo} \\ & = (62 \times 10^4 \times 250) / (1.1 \times 10^6) \\ & = 140.7\text{KNm} \end{aligned}$$

$$\begin{aligned} T_{dg} & = f_y A_g / \gamma_{mo} \\ & = 250 \times 6500 / 1.10 \times 1000 \end{aligned}$$

$$= 1477.3 \text{KN}$$

Design strength due to rupture of critical section,

$$\begin{aligned} T_{dn} &= 0.9 f_y A_n / \gamma_{mi} \\ &= (0.9 \times 415 \times 6500) / (1.25 \times 1000) \\ &= 1942.2 \text{ KN} \end{aligned}$$

The design strength $T_d = 1477.3 \text{ KN}$

Step 2 Check for resistance of cross section to combined effects

Using the interaction equation ,

$$[N/N_d + M_x/M_{dx} + M_y/M_{dy}] \leq 1.0$$

$$\begin{aligned} N_d &= A_g f_y / \gamma_{mo} \\ &= 6500 \times 250 / 1.1 \times 1000 \\ &= 1477.3 \text{ KN} \end{aligned}$$

$$M_x = 50 \text{KNm and}$$

$$M_{dx} = 140.7 \text{ KNm}$$

$$\therefore [600/1477.3 + 50/140.7] = 0.756 < 1$$

Hence safe

Step 3 : Check for lateral torsional buckling resistance

Reduced effective moment is computed as,

$$\begin{aligned} M_{eff} &= [M - \Psi_t Z_{ec} / A] \leq M_d \\ &= [(50 \times 10^6) - (0.8 \times 600 \times 10^3 \times 619 \times 10^3) / 6500] \\ &= 4.3 \times 10^6 \text{ Nmm} \\ &= 4.3 \text{ KNm} < 127.3 \text{KNm} \end{aligned}$$

Step 4 Check for overall buckling strength

$$[P/P_{dx} + M_{eff}/M_{dx}] \leq 1.0$$

$$[600/1477.3 + 4.3/127.3] = 0.439 < 1.0$$

Hence safe

