

⑧

Relation ship between power, Energy and time

$$P = \frac{E}{T}$$

what is the power in watts if energy equal to 50 J is used in 2.5 sec?

$$P = \frac{E}{T} = \frac{50}{2.5} = 20 \text{ watts.}$$

ohm's law:- It describes the fundamental relationship between voltage, current and resistance in an electrical circuit.

deyn:- It states that the current through a conductor is directly proportional to the voltage across it and inversely proportional to its resistance.

mathematical Rep:-

$$V = IR$$

V = Voltage in volts (V)

I = Current in amperes (A)

R = Resistance in ohms (Ω)

(9)

Limitations of ohm's law.

- This law is applicable only for constant temperature
- not applicable for all non-metallic ^{graphite} conductors
- not applicable for non-linear devices such as zener diode, voltage regulator etc

Pbm 1

A 100Ω resistance is directly switched on across a $10V$ battery, what is the current through the resistor? How much is the power loss? Also find the energy consumed in 5 sec.

Soln

given

voltage = $10V$.

Resistance = 100Ω .

time = 5 sec.

By ohm's law,

$$V = IR \Rightarrow I = \frac{V}{R} = \frac{10V}{100} = 0.1A$$

$$\begin{aligned} \text{Power loss} &= VI = IR \times I = I^2 R = (0.1)^2 \times 100 \\ &= 0.01 \times 100 \\ &= 1W. \end{aligned}$$

$$\text{Energy consumed} = PT = 1 \times 5 = 5Ws$$

10) 2) A 560Ω resistor is connected to a circuit which causes a current of 42.4mA to flow through it. Calculate the voltage across the resistor and the power it is dissipating.

Given $R = 560\Omega$

$I = 42.4\text{mA}$

To find voltage & power dissipation.

By Ohm's law,

$$V = IR$$

$$= 42.4 \times 10^{-3} \times 560$$

$$\boxed{V = 23.744\text{V}}$$

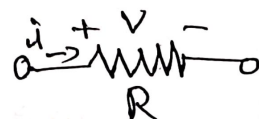
Power $P = VI$

$$= 23.744 \times 42.4 \times 10^{-3} \text{ W}$$

$$= 1.006\text{W}$$

2) For the circuit shown calculate R if $i = -2\mu\text{A}$

and $V = -44\text{V}$



$$R = \frac{V}{I} = \frac{-44}{-2 \times 10^{-6}} = 22 \times 10^6 = 22\text{M}\Omega$$

4) .

11) The power absorbed by the resistor if $V=1V$ and $R=2k\Omega$.

Soln

Ans

$$V=1V$$
$$R=2k\Omega$$

$$P=VI$$

$$P=I^2R$$

$$P=\frac{V^2}{R}$$

By Ohm's Law $V=IR$

$$\Rightarrow I=\frac{V}{R}$$

$$\text{Power} = VI$$
$$= V \cdot \frac{V}{R}$$
$$= \frac{V^2}{R}$$

$$= \frac{1^2}{2k} = 0.5 \times 10^{-3}$$

$$= 0.5 \times 10^{-3} \text{ watt}$$

$$P = 500 \mu\text{watt}$$

5) If $i=3nA$ and $R=4.7M\Omega$ calculate power absorbed.

$$i=3nA, R=4.7M\Omega$$

$$P=V \cdot I$$

$$= IR \cdot I = I^2 R = (3n)^2 \times 4.7M$$

$$= 9 \times 10^{-9} \times 10^9 \times 4.7 \times 10^6$$

$$= 42.3 \times 10^{-12} \text{ W} = 42.3 \text{ pW}$$

②

Relation ship b/w resistance and resistivity.

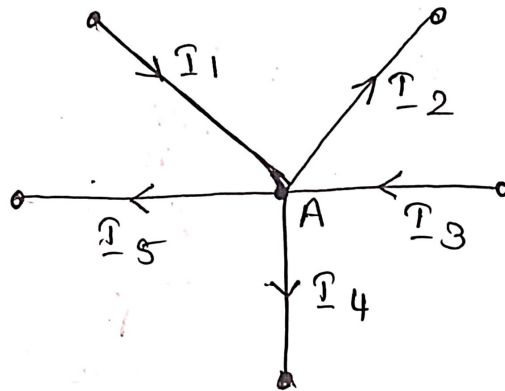
$$R = \rho \cdot \frac{l}{A}$$

$G \rightarrow$ conductance = $\frac{1}{\text{Resistance}}$.

Kirchoff's current law:-

The algebraic sum of the current entering any node is zero.

ie) there is no accumulation of charges at nodes.



In other term current flowing towards the junction is equal to current flowing away from the junction.

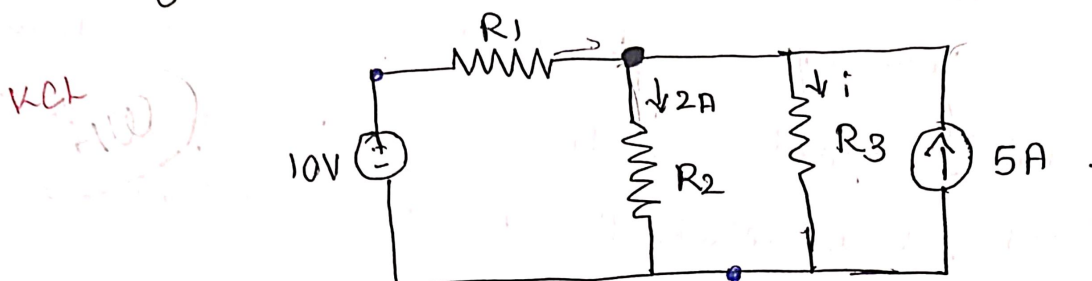
$$I_1 + I_3 = I_2 + I_4 + I_5$$

or) $I_1 - I_2 + I_3 - I_4 - I_5 = 0$.

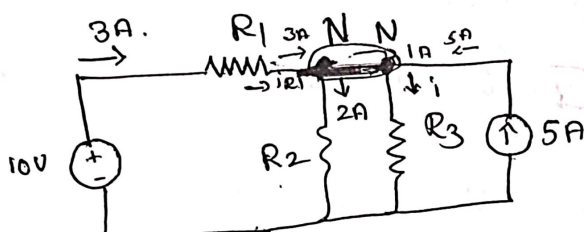
Node: point where two (or) more circuit elements meet.

Branch: current flowing path b/w two nodes.

- 7) For the circuit shown below calculate the current through the resistor R_3 if it is known that the voltage source supplies a current of 3A.



soln



Ans = 6A

Apply KCL at N.

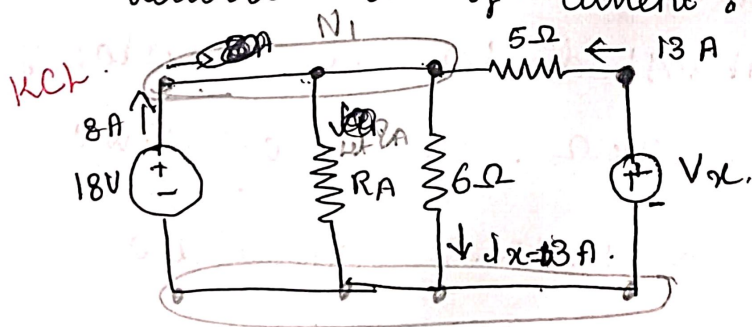
$$\overset{(3)}{i_{R1}} + 5A = 2A + i$$

$$8 - 2 = i \Rightarrow 6A$$

$i = 6A$

Total i in the circuit is
 $3A + 5A = 8A$

- 8) Count the number of branches and nodes in the following circuit if $i_x = 3A$ and the 18V source delivers 8A of current. What is the value of R_A ?



$N = 3$ $B = 5$

Apply KCL at N_1

$$8 + 13 = i_{RA} + 3A$$

$$21 = i_{RA} + 3A$$

$i_{RA} = 18A$

$R_A = \frac{V}{I} = \frac{18V}{18A} = 1\Omega$

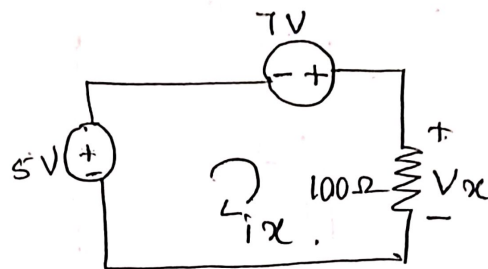
Kirchoff's voltage law: Algebraic sum of the vty around any closed path is zero.

9) Find V_x and I_x .

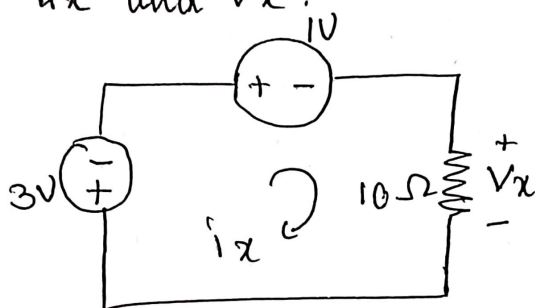
KVL
 $+5V + 7V - V_x = 0$
 $V_x = 12V$

$$I_x = \frac{V_x}{R_x} = \frac{12V}{100} = 0.12A.$$

$$= 120mA.$$



10) Find i_x and V_x .

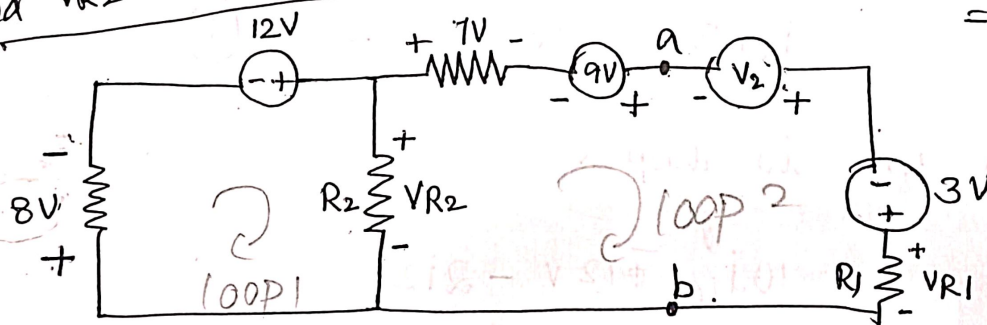


KVL
 $-3V - 1V - V_x = 0$
 $V_x = -4V$

$$i_x = \frac{-4}{10} = -0.4A.$$

$$= 400mA.$$

11. And V_{R2} & V_2 if $V_{R1} = 1V$



Find V_{R2} and V_2 if $V_{R1} = 1V$.

Apply KVL at loop 1

$$(-8V) + 12V - V_{R2} = 0.$$

$$4 = V_{R2}$$

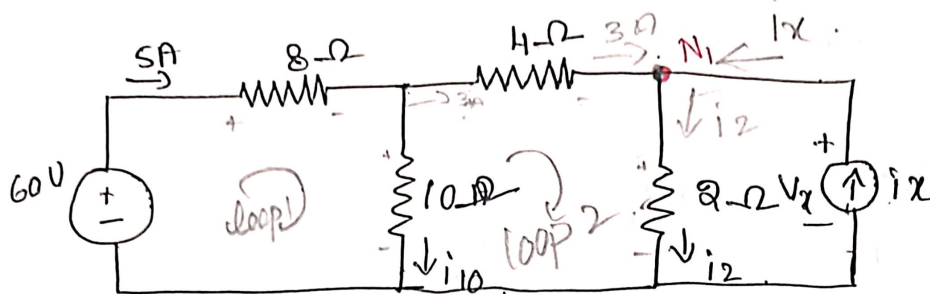
Apply KVL to loop 2

$$-7 + 9 + V_2 + 3 - V_{R1} + V_{R2} = 0$$

$$-7 + 9 + V_2 + 3 - 1 + 4 = 0$$

$$8 + V_2 = 0 \implies V_2 = -8V$$

12. Find V_x in the ckt.



Apply KVL to loop 1

$$60V - 40 - 10i_{10} = 0.$$

$$20 = 10i_{10}$$

$$i_{10} = \frac{20}{10} = 2A.$$

$$\boxed{i_{10} = 2A}$$

Since $5 - i_{10} = 5 - 2 = 3A$ ct flow through 4Ω .

Apply KVL to loop 2.

$$10i_{10} - 12V - 2i_2 = 0$$

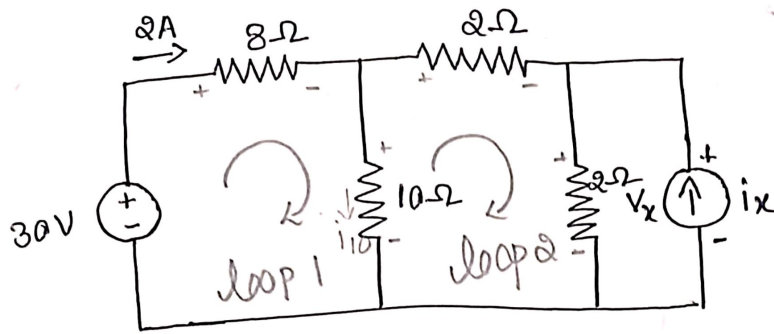
$$20 - 12 - 2i_2 = 0$$

$$8 = 2i_2 \Rightarrow i_2 = \frac{8}{2} \Rightarrow \boxed{i_2 = 4A}$$

$$V_x = 2 \times i_2$$

$$= 2 \times 4 = 8V$$

13.

Determine V_x .SolnApply KVL to loop 1

$$30V - 16V - 10i_{10} = 0$$

$$14V - 10i_{10} = 0$$

$$10i_{10} = 14$$

$$i_{10} = \frac{14}{10}$$

$$i_{10} = 1.4A$$

Apply KVL to loop 2

$$14 - 1.2 - 2i_2 = 0$$

$$12.8 = 2i_2$$

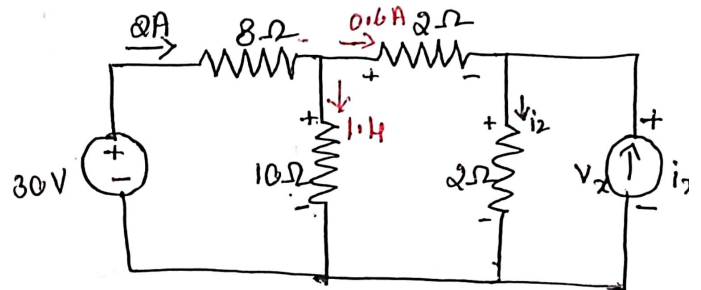
$$i_2 = \frac{12.8}{2} = 6.4$$

$$i_2 = 6.4A$$

$$V_x = i_2 \times 2\Omega$$

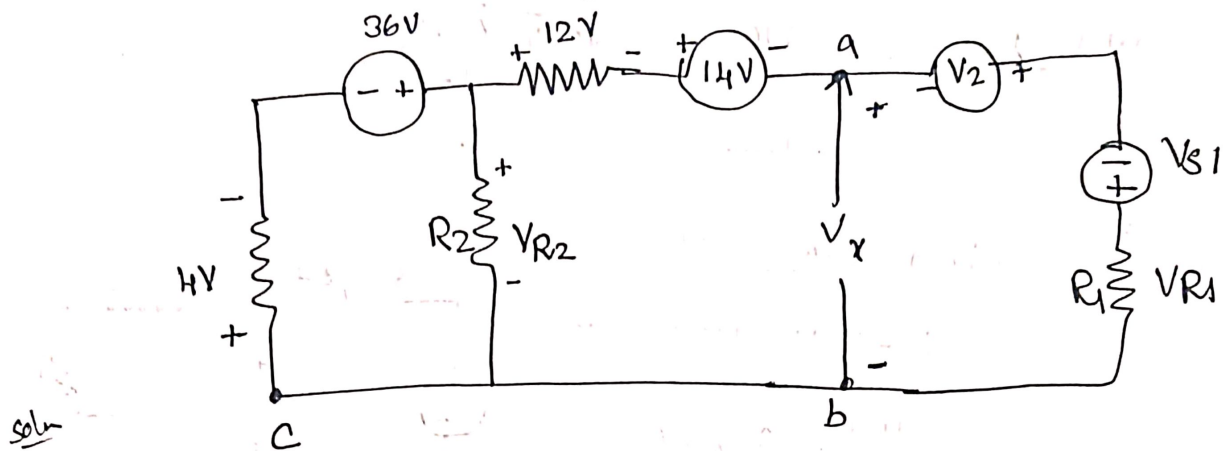
$$= 6.4 \times 2$$

$$V_x = 12.8V$$



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14) For the given circuit calculate V_{R2} & V_x



soln

Apply KVL to loop 1

$$-4V + 36 - V_{R2} = 0$$

$$32 - V_{R2} = 0$$

$$V_{R2} = 32$$

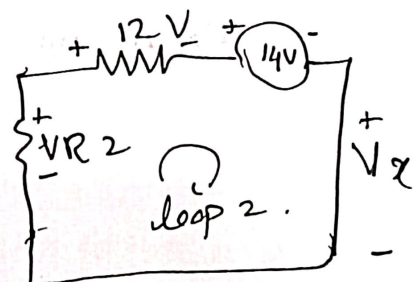
Apply to loop 2.

$$V_{R2} - 12V - 14V - V_x = 0$$

$$32 - 26 - V_x = 0$$

$$6 - V_x = 0$$

$$V_x = 6$$



DC circuit: A DC circuit is a closed electrical circuit where current flow in one direction typically from positive terminal to negative terminal of the power source like a battery. DC circuit

series ckt: In this type of ckt all the element in the circuit carry the same current

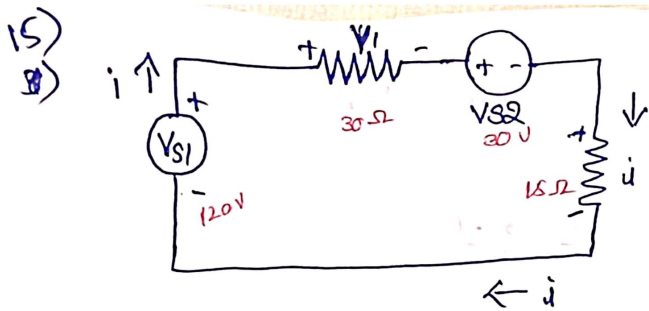
parallel ckt

Apply KVL

$$V_{S1} - iR_1 - V_{S2} - iR_2 = 0$$

$$V_{S1} - V_{S2} = iR_1 + iR_2 \Rightarrow i = \frac{V_{S1} - V_{S2}}{R_1 + R_2}$$





DC Circuits

$V_{S1} = 120V$, $V_{S2} = 30V$, $R_1 = 30\Omega$, $R_2 = 15\Omega$ compute power absorbed by each element.

Soln

We can find $i = \frac{120}{30} = 4A$
Apply KVL to loop.

$$120V - 30i - 30 - 15i = 0$$

$$90V - 45i = 0$$

$$45i = 90$$

$$\boxed{i = 2A}$$

$$\begin{aligned} \text{Power across } V_{S1} &= P_{V_{S1}} = V \times I = 120 \times 2 = 240W \\ P_{30\Omega} &= I^2 R = 2^2 \times 30 = 120W \end{aligned} \quad \left| \quad \begin{aligned} P_{V_{S2}} &= 2 \times 30 = 60W \\ P_{15\Omega} &= 4 \times 15 = 60W \end{aligned} \right.$$

16) Find power absorbed in each element

Apply KVL

$$120V - 30i - 2VA - VA = 0.$$

$$120V - 30i - 3VA = 0 \quad \text{--- (1)}$$

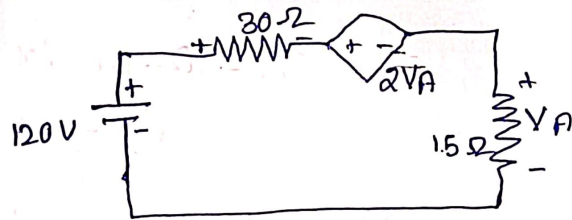
WKT $-VA = 15i \quad \text{--- (2)}$

sub (2) in (1),

$$120V - 30i - 3(-15i) = 0$$

$$120V - 30i + 45i = 0$$

$$120V + 15i = 0 \quad i = \frac{-120}{15} = -8A.$$



$$\boxed{i = -8A}$$

$$\therefore VA = -15 \times 8 = -120$$

$$P_{120} = 120 \times 8 = 960W$$

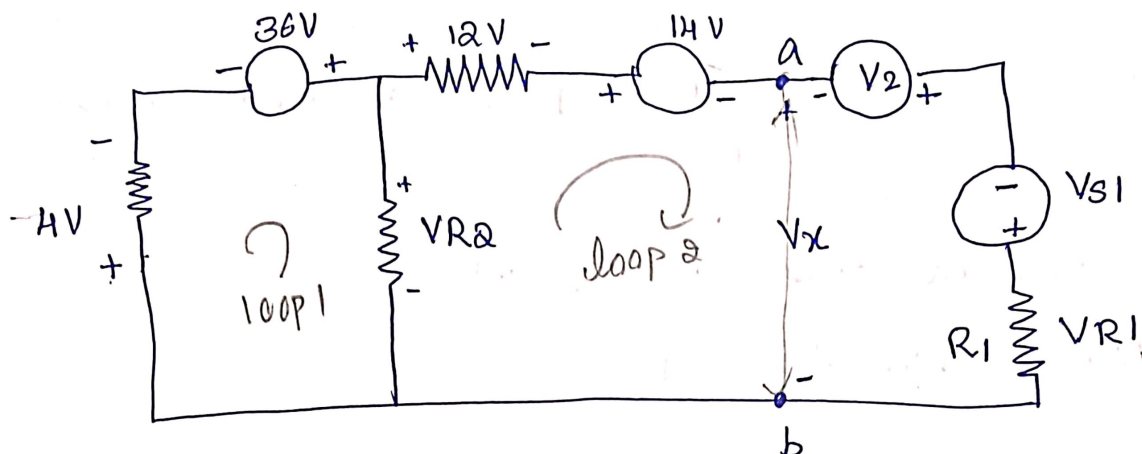
$$P_{30\Omega} = 8^2 \times 30 = 64 \times 30 = 1920W$$

$$P_{2VA} = 8 \times 2 \times 120 = -1920W$$

$$P_{15\Omega} = 8^2 \times 15 = 960W$$

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1) For the given circuit calculate V_{R2} and V_x .



Apply KVL to loop 1

$$-4V + 36V - V_{R2} = 0$$

$$32 - V_{R2} = 0$$

$$\boxed{V_{R2} = 32V}$$

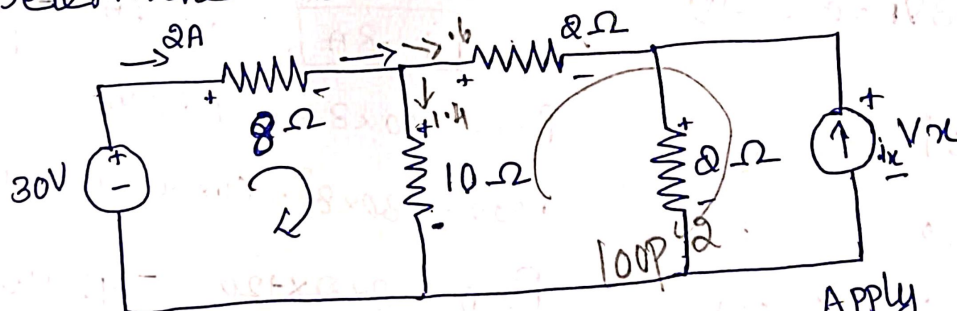
Apply KVL to loop 2.

$$V_{R2} - 12V - 14 - V_x = 0$$

$$32 - 12 - 14 - V_x = 0$$

$$6V - V_x = 0 \Rightarrow \boxed{V_x = 6V}$$

2) Determine V_x in the circuit.



Soln Apply KVL to loop 1

$$30V - 16V - V_{10} = 0$$

$$\boxed{V_{10} = 14V}$$

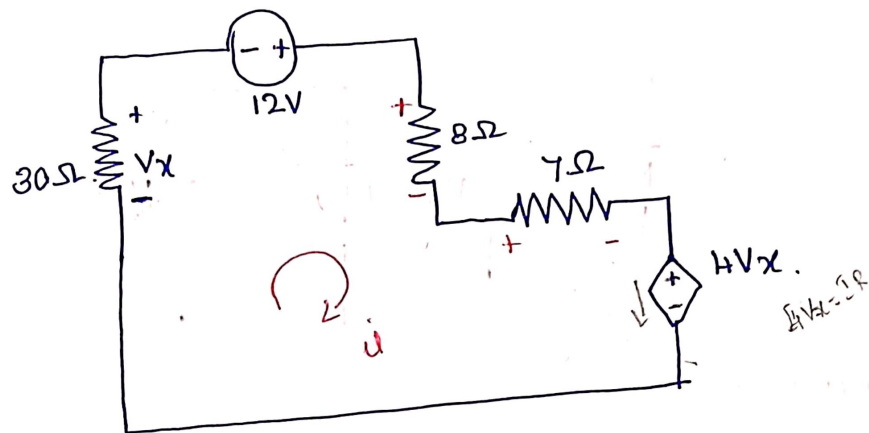
Apply KVL to loop 2

$$+V_{10} - V_{R2} - V_x = 0$$

$$14V - (0.6 \times 2) = V_x$$

$$\boxed{V_x = 12.8V}$$

17. Find the power absorbed by each of the five elements in the following circuit. (20)



Solution

* mark polarity:

* For series dc circuit the current flowing through the entire circuit is same let it be i

* Apply KVL

$$V_x + 12V - 8i - 7i - 4V_x = 0.$$

$$-30i + 12V - 15i - (4 \times 30i) = 0$$

$$-30i + 12V - 15i + 120i = 0$$

$$-45i + 120i = -12$$

$$75i = -12$$

$$i = \frac{-12}{75} = -0.16A$$

$$[\because V_x = -30i]$$

$$P_{30\Omega} = I^2 R = (0.16)^2 30 = 0.768 \text{ watts}$$

$$P_{12V} = V(I) = 12 \times 0.16 = +1.92 \text{ watts}$$

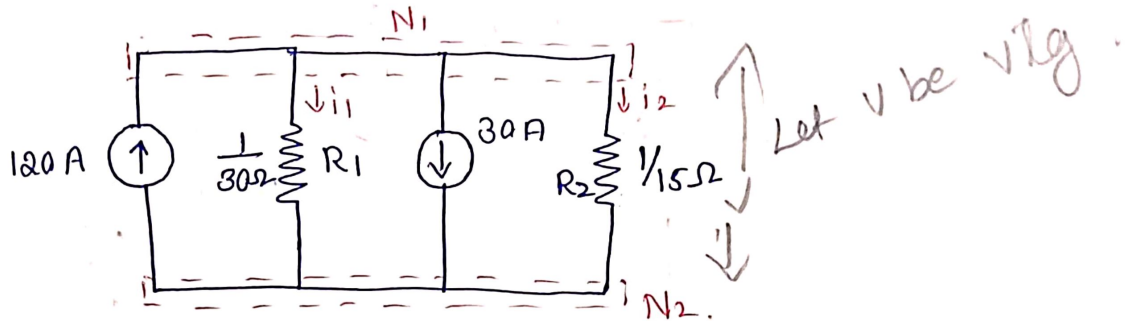
$$P_{8\Omega} = I^2 R = (-0.16)^2 8 = 0.2048 \text{ W}$$

$$P_{7\Omega} = I^2 R = (-0.16)^2 7 = 0.1792 \text{ W}$$

$$P_{4V_x} = 4V_x I = 4(-30 \times -0.16)(-0.16) = -3.072$$

(28)

18. Find the voltage, current and power associated with each element.



Solution:-

There are two nodes in the circuit

Apply KCL

$$\sum \text{current entering } N_1 = \sum \text{current leaving } N_1$$

$$120 = i_1 + 30 + i_2$$

$$i_1 + i_2 = 90$$

$$\frac{V}{1/30} + \frac{V}{1/15} = 90$$

$$30V + 15V = 90$$

$$45V = 90$$

$$V = \frac{90}{45}$$

$$\Rightarrow \boxed{V = 2V}$$

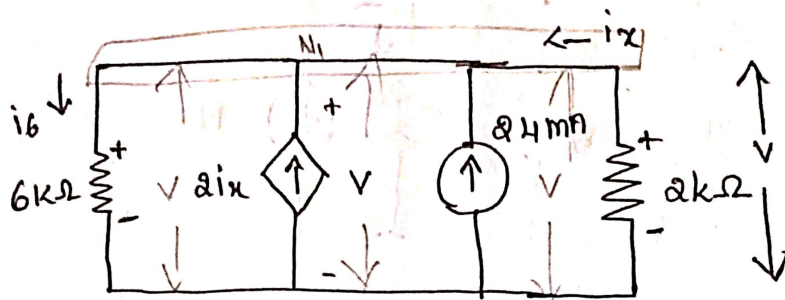
$$P_{120A} = VI = 2 \times 120 = 240 \text{ watts}$$

$$P_{1/30S} = \frac{V^2}{R} = \frac{4}{1/30} = 4 \times 30 = 120 \text{ watts}$$

$$P_{30A} = VI = 2 \times 30 = 60 \text{ watts}$$

$$P_{1/15S} = \frac{V^2}{R} = 4 \times 15 = 60 \text{ watts}$$

19. Determine the value of v and the power supplied by the independent current sources. (22)



Soln

Apply KCL at node 1.

$$2i_x + 24\text{mA} + i_x = i_b$$

$$3i_x - i_b + 24\text{mA} = 0 \quad \text{--- (1)}$$

To know i_x , i_b from fig

For 11th circuits voltage is same

$$\cancel{i_x} \quad \boxed{i_x = \frac{-v}{2k}} \quad , \quad i_b = \frac{v}{6k} \quad \text{--- (3)}$$

sub (2) & (3) in (1) $\Rightarrow$

$$-3 \times \frac{v}{2k} - \frac{v}{6k} + 24\text{mA} = 0$$

$$v \left[\frac{-9-1}{6k} \right] = -24\text{mA}$$

$$v = \frac{-10}{6k} = -24\text{mA}$$

$$P_{24} = v \times 24\text{mA} = 14.4 \times 24\text{mA}$$

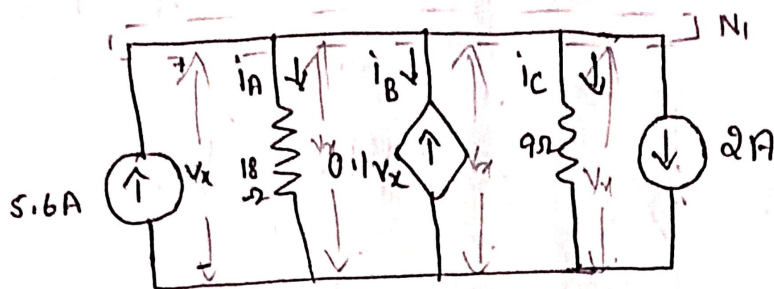
$$\boxed{P_{24} = 345.6\text{mW}}$$

$$v = \frac{6k \times \frac{12}{10^5}}{5} = \frac{72}{5} = 14.4\text{V}$$

$$\boxed{v = 14.4\text{V}}$$

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For the single node pair ckt find i_A , i_B & i_C .



Apply KCL at N_1 ,

$$5.6 = i_A + i_B + i_C + 2 \quad 5.6 + 0.1V_x = i_A + i_C + 2$$

$$3.6 = i_A + i_B + i_C \quad 5.6 + 0.1V_x = \frac{V_x}{18} + \frac{V_x}{9} + 2$$

$$= \frac{V_x}{18} + 0.1V_x + \frac{V_x}{9}$$

$$= \frac{V_x + 2V_x}{18} - 0.1V_x \quad 3.6 + 0.1V_x = \frac{2V_x + V_x}{1}$$

$$= \frac{3V_x}{18} - 0.1V_x$$

$$3.6 = \frac{3V_x}{18} - 0.1V_x$$

$$3.6 = V_x \left(\frac{1}{6} - 0.1 \right)$$

$$3.6 = \frac{3V_x - 1.8V_x}{18}$$

$$= V_x (0.166 - 0.1)$$

$$64.8 = 1.8 V_x \Rightarrow V_x = 54 \text{ mV}$$

$$\frac{3.6}{0.066} = V_x$$

$$\boxed{V_x = 54 \text{ mV}}$$

$$0.066$$

$$\boxed{V_x = 54.54 \text{ mV}}$$

$$i_A = \frac{V_x}{18} = \frac{54}{18} = 3 \text{ A}$$

$$i_C = \frac{V_x}{9} = \frac{54}{9} = 6 \text{ A}$$

$$i_B = -0.1V_x = -5.4 \text{ A}$$