

Self Inductance and Mutual Inductance

When a coil with 'N' turns, carrying current I, the flux is produced by it. This flux links with each turn of the coil. Thus total flux linkage of the coil having N turn is $N\Phi$ wb-turns.

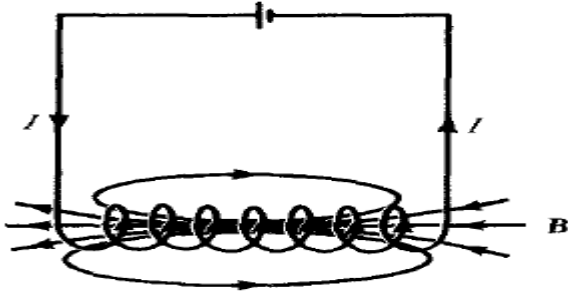


Fig : Magnetic Field produced by a circuit

The ratio of the flux linkage to the current producing that flux is called inductance 'L'. It is measured in henry (H).

$$L = \frac{N\Phi}{I} \text{ H}$$

In general inductance is also referred as self inductance. The flux produced by the current flowing through the coil links with the coil itself.

Inductance of Solenoid:

Let the current flowing through the solenoid be I ampere. The length of the solenoid be l and the cross sectional area be A.

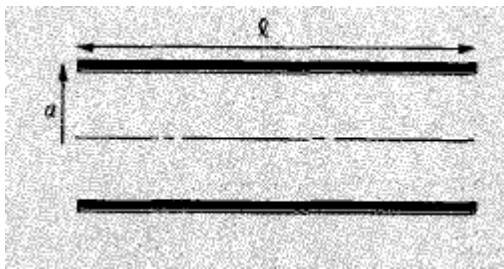


Fig : Solenoid

$$H = \frac{NI}{l} \text{ A/m}$$

The total flux linkage is given by,

$$\text{The total flux linkage} = N\Phi = N(B)(A)$$

$$= N\mu HA$$

$$\text{Total flux linkage} = \mu NHA$$

$$= \mu N \left[\frac{NI}{l} \right] A$$

$$\frac{\mu N^2 IA}{l}$$

Thus the inductance of the solenoid is given by,

$$L = \frac{\text{total flux linkage}}{\text{total current}}$$

$$L = \frac{\mu N^2 IA}{l(I)}$$

$$L = \frac{\mu N^2 A}{l} H$$

Inductance of the toroid:

Consider a toroidal ring with N turns and carrying current I. The magnetic flux density inside a toroidal ring is

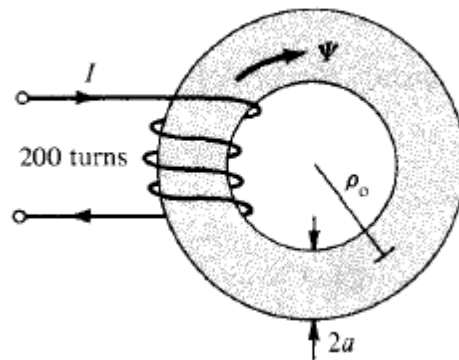


Fig : Toroid ring

$$B = \frac{\mu NI}{2\pi R}$$

The total flux linkage, cross sectional view of a toroidal ring having N turns is given by ,

$$\text{Total flux linkage} = N\Phi$$

$$\Phi = B \cdot A, \quad A \rightarrow \text{area of cross section of a toroidal ring}$$

$$\text{Total flux linkage} = N(B)(A)$$

$$= N \left(\frac{\mu NI}{2\pi R} \right) A$$

$$\text{Total flux linkage} = \frac{\mu N^2 IA}{2\pi R}$$

The inductance of a toroid is given by,

$$L = \frac{\text{total flux linkage}}{\text{total current}}$$

$$L = \frac{\mu N^2 I A}{2\pi R \cdot I} = \frac{\mu N^2 A}{2\pi R} \text{ H}$$

$$A = \pi r^2 m^2$$

For a toroid with N number of turns h as the height of toroid with r_1 as inner radius and r_2 as outer radius the inductance is given by

$$L = \frac{\mu N^2 H}{2\pi} \ln \left[\frac{r_2}{r_1} \right] \text{ H}$$