

**ROHINI COLLEGE OF ENGINEERING AND TECHNOLOGY**  
**Approved by AICTE & Affiliated to Anna University**  
**Accredited with A<sup>+</sup> grade by NAAC**  
**DEPARTMENT OF MECHANICAL ENGINEERING**



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**NAME OF THE SUBJECT: ENGINEERING MECHANICS**

**SUBJECT CODE : ME3351**

**REGULATION 2021**

**UNIT V: FRICTION**



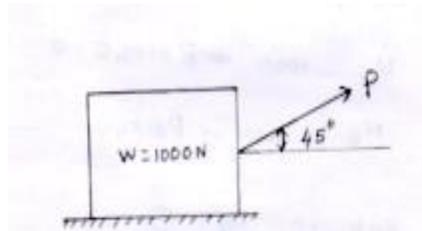
Friction:



Problem based on Friction:

1. A body weighting 1000N is lying on a horizontal plane. Determine the necessary force to move the body along the plane if the force is applied at angle of  $45^\circ$  to the horizontal with the coefficient of friction 0.24

Given:

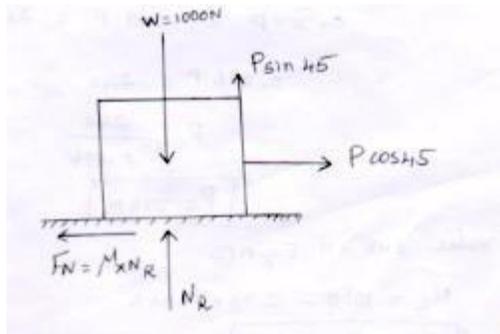


Coefficient of friction  $\mu = 0.24$

Weight of body  $w = 1000\text{ N}$

To find

Soln



Sum of X Direction Force +  $\longrightarrow$  -  $\longleftarrow$

$$\sum F_x = 0$$

$$P \cos 45 - F_N = 0$$

$$P \cos 45 - \mu \times N_R = 0$$

$$P \cos 45 - 0.24 \times N_R = 0 \text{ ----- (1)}$$



Sum of Y direction force  $\uparrow + \quad -$   
 $\Sigma F_y = 0$

$$N_R - 1000 + P \sin 45 = 0$$

$$N_R = 1000 + P \sin 45 = 0$$

$N_R$  value sub in Eqn(1)

$$P \cos 45 - 0.24 \times [1000 - P \sin 45] = 0$$

$$P \cos 45 - 240 + [P \sin 45 \times 0.24] = 0$$

$$0.707P + 0.169P = 240$$

$$0.876P = 240$$

$$P = \frac{240}{0.876}$$

$$P = 273N$$

P value sub in eqn (2)

$$N_R = 1000 - 273 \times \sin 45$$

$$N_R = 806.95 N$$

Problem: 2

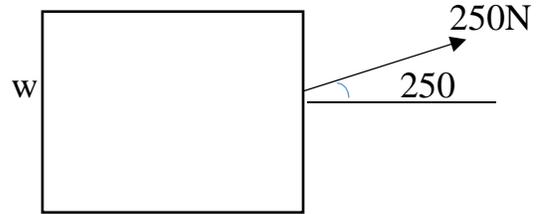
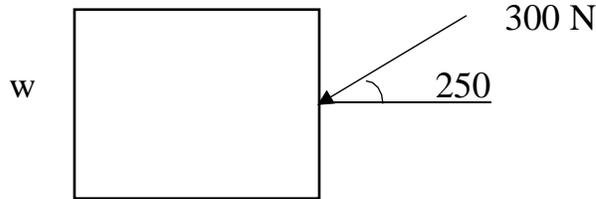
A pull of 250N inclined at  $25^\circ$  to the horizontal plane is required just to move a body kept on a rough horizontal plane. But the push required just to move the body is 300N. If the push is inclined at  $25^\circ$  to the horizontal. Find the weight of the body and the coefficient of friction b/w the body and the plane.

Given:

$$P_1 = \text{pull load} = 250 N \text{ at } 25^\circ$$

$$P_2 = \text{push load} = 300 N \text{ at } 25^\circ$$

To find

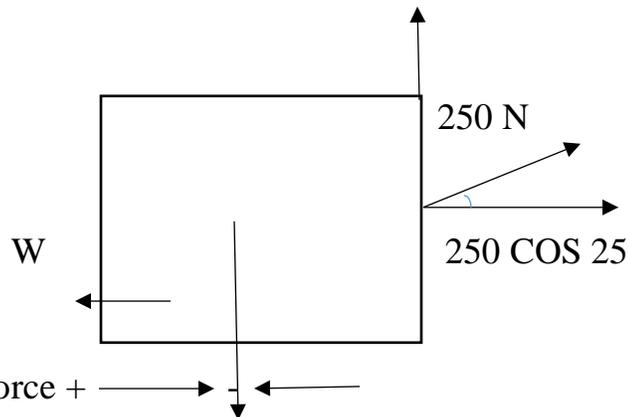


Weight and coefficient of friction

Soln

Case (i)

Free body diagram



Sum of x directional force +  $\rightarrow$   $\leftarrow$

$$\sum F_x = 0$$

$$250 \cos 25^\circ - F_N = 0$$

$$250 \cos 25^\circ - \mu \times N_{R1} = 0$$

$$226.57 - \mu \times N_{R1} = 0$$

$$-\mu \times N_{R1} = -226.57$$

$$\mu \times N_{R1} = 226.57 \text{----- (1)}$$

Sum of Y directional force  $\downarrow$   $\uparrow$  +

$$\sum F_y = 0$$

$$N_{R1} - W + 250 \sin 25 = 0$$

$$N_{R1} = W - 250 \sin 25$$

$$N_{R1} = W - 105.65 \text{----- (2)}$$

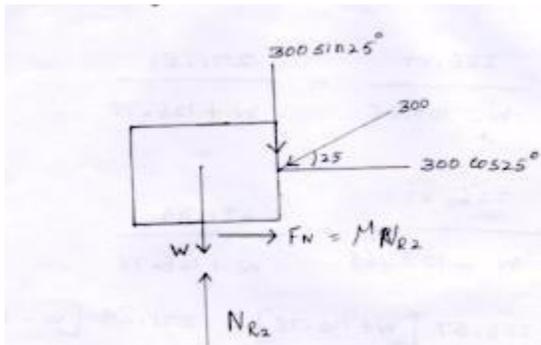
Sub eqn (2), from eqn (1)

$$\mu N_{R1} = 226.57$$

$$\mu = \frac{226.57}{N_{R1}}$$

$$\mu = \frac{226.57}{W - 105.65} \text{----- (3)}$$

Case (2) Free body diagram



Sum of X Directional force  $\sum F_x = 0$

$$F_N - 300 \cos 25^\circ = 0$$

$$\mu N_{R2} = 300 \cos 25^\circ$$

$$\mu N_{R2} = 271.89 \text{N} \text{----- (4)}$$

Sum of vertical force [Y direction]  $\sum F_y = 0$

$$N_{R2} - W - 300 \sin 25^\circ = 0$$

$$N_{R2} = W + 300 \sin 25^\circ$$

$$N_{R2} = W + 126.78$$

$N_{R2}$  value sub in Eqn (4)

$$\mu N_{R2} = 271.89$$

$$\mu = \frac{271.89}{N_{R2}}$$

$$\mu = \frac{271.89}{W + 126.78} \text{----- (5)}$$

Eqn (3) = Eqn (5)

$$\frac{226.57}{W - 105.65} = \frac{271.89}{W + 126.78}$$

$$226.57[W + 126.78] = 271.89[W - 105.65]$$

$$226.57W + 28.72 \times 10^3 = 271.89W - 28.72 \times 10^3$$

$$226.57W - 271.89W = -28.72 \times 10^3 - 28.72 \times 10^3$$

$$-45.32W = -57.44 \times 10^3$$

$$W = \frac{57.44 \times 10^3}{45.32}$$

$$W = 1267.43N$$

W value sub in eqn (3)

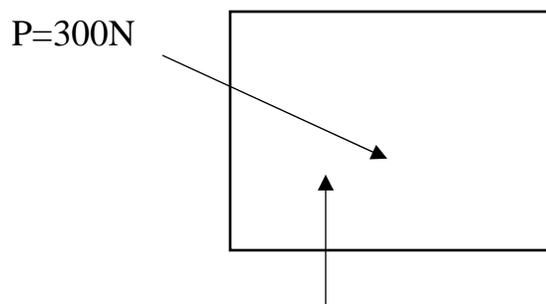
$$\mu = \frac{226.57}{W - 105.65}$$

$$\mu = \frac{226.57}{1267.43 - 105.65}$$

$$\mu = 0.195$$

### Problem 3

Calculate the static coefficient of friction  $\mu_s$  b/w the block shown in fig having a mass of 75kg and the surface. Also find the magnitude and direction of the friction force if the force P applied is inclined at  $45^\circ$  to the horizontal and  $\mu_s = 0.30$



Given:

$$\text{Weight} = 75 \text{ kg} = 75 \times 9.81 = 735.75N$$

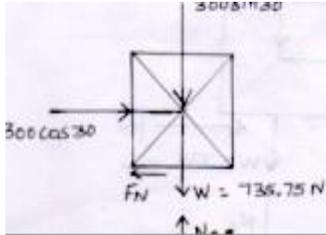
To find

Case (i) Coefficient of friction  $\mu_s$

Case (ii) Frictional force ' $F_N$ ', Direction  $\emptyset$

Soln

Case (i) free body diagram



Sum of all the X direction force  $\sum F_x = 0$

$$300 \cos 30 - F_N = 0$$

$$300 \cos 30 - \mu N_R = 0$$

$$\mu N_R = -300 \cos 30$$

$$\mu N_R = 259.8 \text{----- (1)}$$

Sum of all the Y direction force  $\sum F_y = 0$

$$-300 \sin 30 - 735.75 + N_R = 0$$

$$N_R = 300 \sin 30 + 735.75$$

$$N_R = 885.75 \text{ N}$$

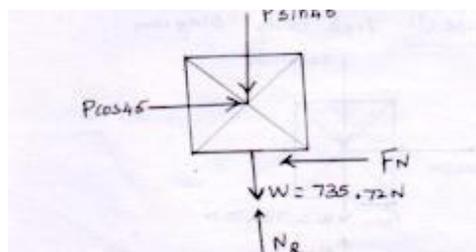
$N_R$  value sub in eqn(i)

$$\mu N_R = 259.8$$

$$\mu = \frac{259.8}{N_R} = \frac{259.8}{885.75}$$

$$\mu = 0.29$$

Case (ii) free body diagram



Sum of all the horizontal force [X direction]  $\sum F_x = 0$

$$P \cos 45 - F_N = 0$$

$$-F_N = -P \cos 45$$

$$F_N = P \cos 45$$

$$\mu N_R = p \cos 45$$

$$N_R = \frac{p \cos 45}{\mu} = \frac{p \cos 45}{0.3}$$

$$N_R = 2.35p$$

Sum of all the Direction force  $\sum F_y = 0$

$$-p \sin 45 - 732.72 + N_R = 0$$

$$-p \times 0.7 - 735.72 + 2.35p = 0$$

$$-0.7p + 2.35p = 735.72$$

$$1.64p = 735.72$$

$$p = \frac{735.72}{1.64}$$

$$p = 447.81N$$

$$N_R = 2.35p$$

$$N_R = 2.35 \times 447.81$$

$$N_R = 1052.37N$$

$$F_N = \mu \times R = 0.3 \times 1052.37$$

$$F_N = 315.71N$$

Direction  $\phi$

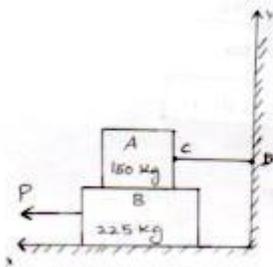
$$\phi = \tan^{-1} \left[ \frac{F_N}{N_R} \right]$$

$$\phi = \tan^{-1} \left[ \frac{315.71}{1052.37} \right]$$

$$\phi = 16^{\circ}41'$$

Problem 4:

Determine the smallest force  $P$  required to move the block B shown in fig below (i) block A is restrained by cable CD as shown in fig. (ii) Cable CD is removed. Take  $\mu_s = 0.30$  and  $\mu_k = 0.25$



Given:

$$W_A = 150kg = 150 \times 9.81 = 1471.5N$$

$$W_B = 225kg = 225 \times 9.81 = 2207.25N$$

$$\mu_s = 0.3$$

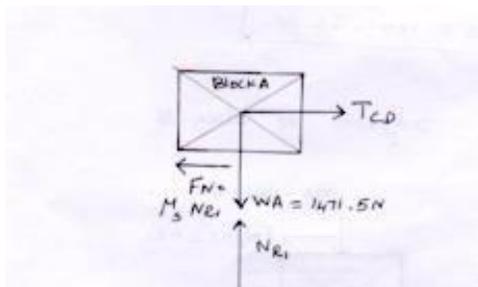
$$\mu_k = 0.25$$

To find

Force  $P$

Soln

Block A is restrained by cable CD



Sum of X direction force  $\Sigma = 0$

$$T_{CD} - F_N = 0$$

$$T_{CD} - \mu_s N_{R1} = 0$$

$$T_{CD} = \mu_s N_{R1}$$

$$T_{CD} = 0.3 N_{R1} \text{----- (1)}$$

Sum of vertical [Y direction force]  $\Sigma F_y = 0$

$$N_{R1} - W_A = 0$$

$$N_{R1} = W_A$$

$$N_{R1} = 1471.5 N$$

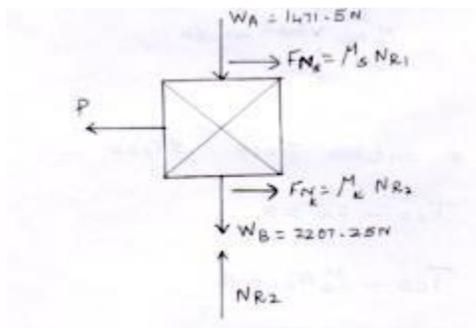
$N_{R1}$  value sub in eqn(i)

$$T_{CD} = 0.3 R_1$$

$$T_{CD} = 0.3 \times 1471.3$$

$$T_{CD} = 441.45 N$$

Free body diagram of block B



Sum of X direction force

$$F_{N_s} + F_{N_k} - p = 0$$

$$\mu_s N_{R1} + \mu_k N_{R2} - p = 0$$

$$p = \mu_s N_{R1} + \mu_k N_{R2} \text{----- (1)}$$

Sum of Y direction force

$$-1471.5 - 2207.25 + N_{R2} = 0$$

$$N_{R2} = 1471.5 + 2207.25$$

$$N_{R2} = 3678.75N$$

$N_{R2}$  value sub in Eqn (1)

$$p = \mu_s N_{R1} + \mu_k N_{R2}$$

$$p = 0.3 \times 1471.5 + 0.25 \times 3678.75$$

$$p = 1361.14 N$$

(i) Cable CD is removed

Both block is removed

Both the block will consider as a single body

$$p = F_N$$

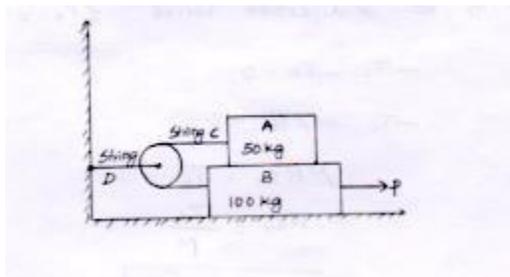
$$p = \mu_k N_{R2} = 0.25 \times 3678.75$$

$$p = 919.68N$$

Problem-6

Two blocks A and B of mass 50 kg and 10 kg respectively are connected by a string c which passes through a frictionless pulley connected with the fixed wall by another string D as shown in fig. Find the force P required to pull the block B. also find the tension in the string D.

Take coefficient of friction at all contact surface as 0.3°



Given:

$$\text{Weight of block A } W_A = 50kg = 50 \times 9.81 = 490.5N$$

$$\text{Weight of block B } W_B = 100kg = 100 \times 9.81 = 981N$$

$$\text{Coefficient of friction } \mu = 0.3$$

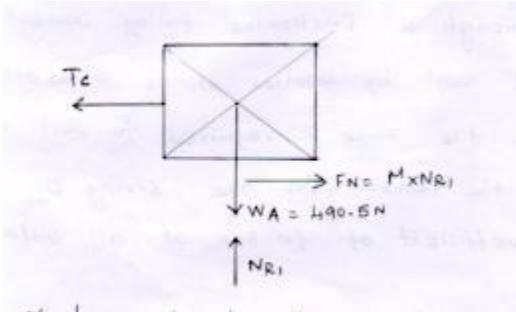
To find

(i) Force P

(ii) Tension in string  $T_D$

Soln

Free body diagram of block A



Sum of x direction forces  $\sum F_x = 0$

$$-T_c - F_N = 0$$

$$-T_c + \mu N_{R1} = 0$$

$$\mu N_{R1} = T_c$$

$$N_{R1} = \frac{T_c}{\mu}$$

$$N_{R1} = \frac{T_c}{0.3} \text{----- (1)}$$

Sum of Y direction force  $\sum F_y = 0$

$$-W_A + N_{R1} = 0$$

$$N_{R1} = W_A$$

$$N_{R1} = 490.5\text{ N}$$

$N_{R1}$  value sub in Eqn (1)

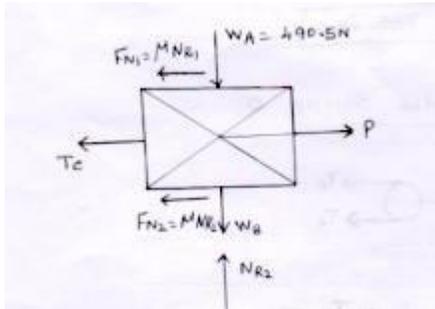
$$N_{R1} = \frac{T_c}{0.3}$$

$$490.5 = \frac{T_c}{0.3}$$

$$T_c = 147.15 \text{ N}$$

Consider block B

free body diagram



Sum of X direction force  $\sum F_x = 0$

$$p - T_c - F_{N1} - F_{N2} = 0$$

$$p - \mu N_{R1} + \mu N_{R2} = 0$$

$$p - 147.15 - 0.3 \times 490.15 - 0.3 \times N_{R2} = 0$$

$$p - 147.15 - 147.04 - 0.3 \times N_{R2} = 0$$

$$p - 294.19 - 0.3N_{R2} = 0$$

$$p = 294.19 - 0.3N_{R2} = 0$$

$$P = 294.19 + N_{R2} \text{----- (2)}$$

Sum of Y direction force  $\sum F_y = 0$

$$N_{R2} - W_B - W_A = 0$$

$$N_{R2} - 981 - 490.5 = 0$$

$$N_{R2} = 1471.5 \text{ N}$$

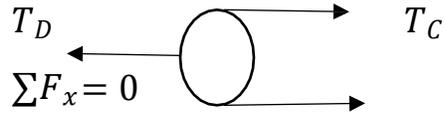
$N_{R2}$  value sub in eqn(2)

$$p = 294.19 + 0.3N_{R2}$$

$$p = 294.19 + 0.3 \times 1471.5$$

$$p = 735.64 \text{ N}$$

Tension in the string D:



$$T_c + T_c - T_D = 0$$

$$2T_c - T_D = 0$$

$$2 \times 147.15 - T_D = 0$$

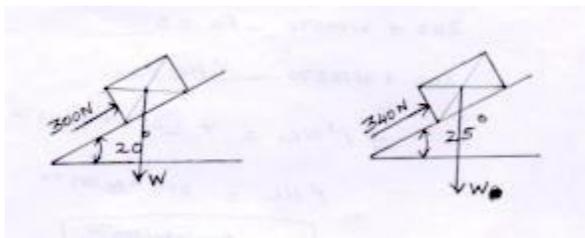
$$294.3 - T_D = 0$$

$$-T_D = -294.3$$

$$T_D = 294.3N$$

Problem -7

A force of 300 n is required just to move a block up a plane inclined at  $20^\circ$ . To the horizontal, the force being applied parallel to the plane shown in fig. if the inclination of the plane is increased to  $25^\circ$ , the force required just to move the block up is 340 N, [the force is acting parallel to the plane]. Determine the weight of the block and coefficient of friction.



Given:

Case (i)

Weight of body  $w=?$

Force on body  $P= 300\text{ N}$  at  $20^\circ$  inclined on plane horizontal

Case (ii)

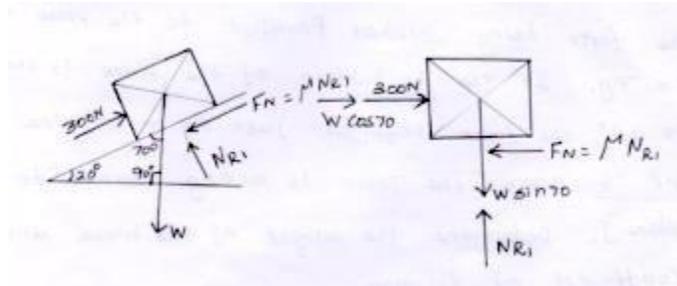
Force on body  $P= 340\text{ N}$  at  $25^\circ$

To find:

Weight of body & coefficient of friction

Soln:

Case (i) free body diagram



Sum of X directional force  $\sum F_X = 0$

$$300 + w \cos 70 - F_N = 0$$

$$300 + w \cos 70 - \mu N_{R1} = 0$$

$$-N_{R1} = -[300 + w \cos 70]$$

$$\mu N_{R1} = 300 + w \cos 70$$

$$\mu = \frac{300 + w \cos 70}{N_{R1}} \text{----- (1)}$$

Sum of all Y direction force  $\sum = 0$

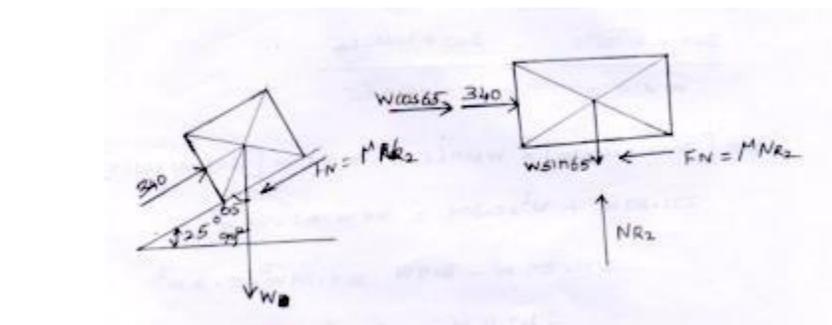
$$N_{R1} - w \sin 70 = 0$$

$$N_{R1} = w \sin 70 \text{----- (2)}$$

$N_{R1}$  value sub in eqn (1)

$$\mu = \frac{300 + w \cos 70}{w \sin 70} \text{----- (3)}$$

Case (ii) consider block 2



Sum of all the X direction force  $\sum F_X = 0$

$$340 + w \cos 65 - F_N = 0$$

$$340 + w \cos 65 - \mu N_{R2} = 0$$

$$-\mu N_{R2} = -[340 + w \cos 65]$$

$$\mu = \frac{340 + w \cos 65}{N_{R2}} \text{----- (4)}$$

Sum of all the Y direction force  $\sum F_Y = 0$

$$N_{R2} - w \sin 65 = 0$$

$$N_{R2} = w \sin 65 \text{----- (5)}$$

Eqn (5) sub in eqn (4)

$$\mu = \frac{340 + w \cos 65}{w \sin 65} \text{----- (6)}$$

Eqn(3) = eqn (6)

$$\frac{300 + w \cos 70}{w \sin 70} = \frac{340 + w \cos 65}{w \sin 65}$$

$$[300 + w \cos 70] \times w \sin 65 = w \sin 70 [340 + w \cos 65]$$

$$271.89w + w^2 \times 0.309 = 319w + 0.39w^2$$

$$271.86w - 319w = 0.39w^2 - 0.3w^2$$

$$-47.11 w = 0.09w^2$$

$$-47.11 w = 0.09w$$

$$w = \frac{-47.11}{0.09}$$

$$\text{ans } w = -523.47 \text{ N}$$

w value sub in eqn(3)

$$\mu = \frac{300 + w \cos 70}{w \sin 70}$$

$$\mu = \frac{300 + (-523.47) \cos 70}{(-523.47) \sin 70}$$

$$\text{Ans } \mu = -0.24$$

### Problem 8

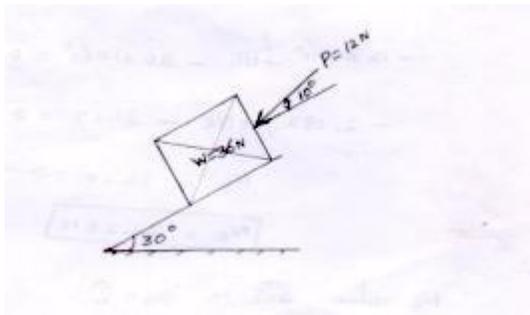
A block weighting 360 n is resting on a rough inclined plane having an inclination of  $30^\circ$ . A force of 12 N is applied at an angle of  $10^\circ$  up and the block is just on the point of moving down the plane. Determine the coefficient of friction

Given:

Block weight  $w=36$  N

Inclination of the plane  $\phi = 30^\circ$

Force on block  $P=12$  N at  $10^\circ$

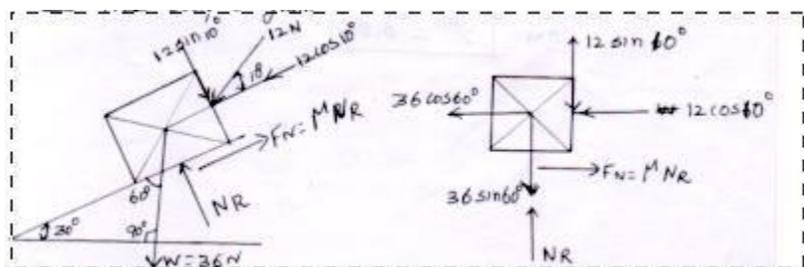


To find

Coefficient of friction  $\mu$

Soln:

Free body diagram



Sum of X direction force  $\sum F_X = 0$

$$-12 \cos 10 - 36 \cos 60 + F_N = 0$$

$$-11.87 - 18 + \mu N_R = 0$$

$$-29.87 + \mu N_R = 0$$

$$\mu N_R = 29.87$$

$$\mu = \frac{29.87}{N_R} \text{----- (1)}$$

Sum of all the Y direction force  $\sum F_y = 0$

$$-12 \sin 10^\circ + N_R - 36 \sin 60^\circ = 0$$

$$-2.083 + N_R - 31.17 = 0$$

$$N_R - 33.25 = 0$$

$$N_R = 33.25 \text{ N}$$

$N_R$  value sub in Eqn (1)

$$\mu = \frac{29.87}{N_R} = \frac{29.87}{33.25}$$

$$\text{ans } \mu = 0.89$$