

5.2.4 MERGE SORT

- Merge Sort is one of the most popular sorting algorithms that is based on the principle of Divide and Conquer Algorithm.
- Here, a problem is divided into multiple sub-problems. Each sub-problem is solved individually. Finally, sub-problems are combined to form the final solution.

Merge Sort Algorithm

- MergeSort is a recursive sorting procedure that uses at most **$O(n \lg(n))$** comparisons.
- To sort an array of **n** elements, we perform the following steps in sequence:
- If **$n < 2$** then the array is already sorted.
- Otherwise, **$n > 1$** , and we perform the following three steps in sequence:
 1. **Sort** the left half of the the array using MergeSort.
 2. **Sort** the right half of the the array using MergeSort.
 3. **Merge** the sorted left and right halves.

Algorithm

Step 1: Start

Step 2: Declare array and left, right, mid

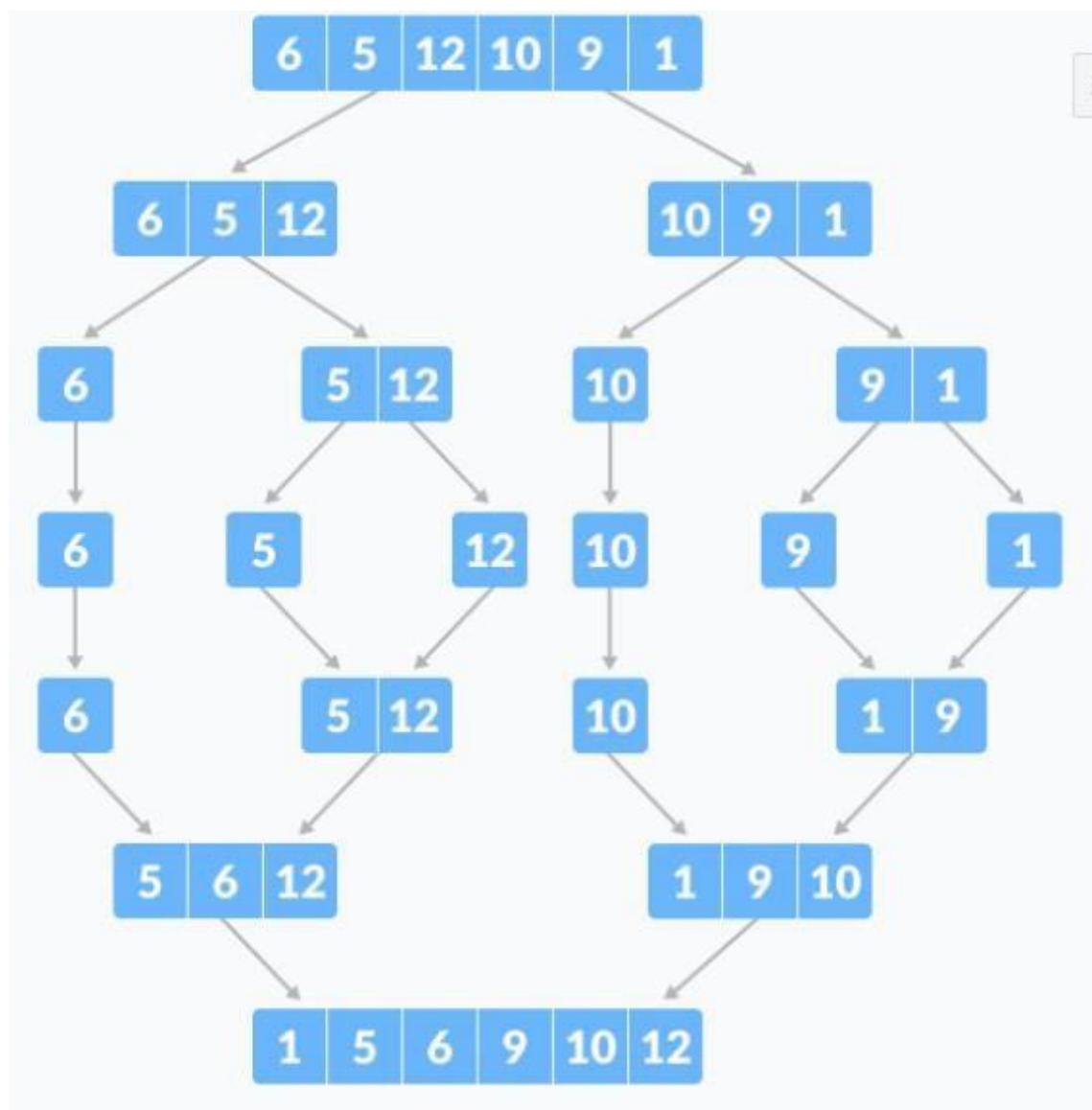
variable Step 3: Perform merge function.

```

if left > right
    return
mid=      (left+right)/2
mergesort(array, left, mid)
mergesort(array,      mid+1,
right) merge(array, left, mid,
right)

```

Step 4: Stop



How to Merge

Here are two lists to be merged:

First: (12, 16, 17, 20, 21, 27)

Second: (9, 10, 11, 12, 19)

Compare **12** and **9**

First: (12, 16, 17, 20, 21, 27)

Second: (10, 11, 12, 19)

New: (9)

Compare **12** and **10**

First: **(12, 16, 17, 20, 21, 27)**

Second: **(11, 12, 19)**

New: (9, 10)

Compare **12** and **11**

First: **(12, 16, 17, 20, 21, 27)**

Second: **(12, 19)**

New: (9, 10, 11)

Compare **12** and **12**

First: **(16, 17, 20, 21, 27)**

Second: **(12, 19)**

New: (9, 10, 11, 12)

Compare **16** and **12**

First: **(16, 17, 20, 21, 27)**

Second: **(19)**

New: (9, 10, 11, 12, 12)

Compare **16** and **19**

First: **(17, 20, 21, 27)**

Second: **(19)**

New: (9, 10, 11, 12, 12, 16)

Compare **17** and **19**

First: **(20, 21, 27)**

Second: (19)

New: (9, 10, 11, 12, 12, 16, 17)

Compare **20** and **19**

First: (20, 21, 27)

Second: ()

New: (9, 10, 11, 12, 12, 16, 17, 19)

Checkout **20** and **empty list**

First: ()

Second: ()

New: (9, 10, 11, 12, 12, 16, 17, 19, 20, 21, 27)

Program

```
void merge(int arr[], int low, int mid, int high)
{
    int i, j, k;
    int temp[50];

    i = low;
    j = mid + 1;
    k = low;

    while (i <= mid && j <= high)
    {
        if (arr[i] <= arr[j])
            temp[k++] = arr[i++];
        else
            temp[k++] = arr[j++];
    }

    while (i <= mid)
```

```

temp[k++] = arr[i++];

while (j <= high)
    temp[k++] = arr[j++];

for (i = low; i <= high; i++)
    arr[i] = temp[i];
}

void mergeSort(int arr[], int low, int high)
{
    int mid;
    if (low < high)
    {
        mid = (low + high) / 2;
        mergeSort(arr, low, mid);
        mergeSort(arr, mid + 1, high);
        merge(arr, low, mid, high);
    }
}

```

Advantages

- Sorts elements **faster even for large data**
- **Same speed in all cases** (best, average, worst)
- Keeps **same order for equal elements**
- Easy to understand using **divide and conquer**
- Works well for **linked lists**

Disadvantages

- Needs **extra memory** for temporary arrays
- Cannot sort in the **same array**
- Takes more time for **small number of elements**
- Uses **recursion**, which needs more memory

Applications

- Used to sort **large amounts of data**
- Used in **database systems**
- Used when **stable sorting** is needed
- Useful in **file sorting**
- Used in **parallel processing**

