3.2 E.M.F EQUATION OF A TRANSFORMER





[Source: "Basic Electrical and Electronics Engineering" by Kothari D.P, Page – 435]

Transformer EMF Equation Let,

 N_A = Number of turns in primary

 $N_B =$ Number of turns in secondary

 $Ø_{max}$ = Maximum flux in the core in

webers = $B_{max} X A f$ = Frequency of

alternating current input in hertz (H_Z)

As shown in figure above, the core flux increases from its zero value to maximum value $Ø_{max}$ in one quarter of the cycle, that is in ¹/₄ frequency second.

Therefore, average rate of change of flux = $Ø_{max}/\frac{1}{4} f = 4f Ø_{max}Wb/s$

Now, rate of change of flux per turn means induced electro

motive force in volts. Therefore, average electro-motive force

induced/turn = 4f $Ø_{max}$ volt

If flux Ø varies sinusoidally, then r.m.s value of induced e.m.f is obtained by

multiplying the average value with form factor.

Form Factor = r.m.s. value/average value = 1.11

Therefore, r.m.s value of e.m.f/turn = 1.11 X 4f

 $Ø_{max} = 4.44 f Ø_{max}$ Now, r.m.s value of induced e.m.f

in the whole of primary winding

= (induced e.m.f./turn) X Number of

primary turns Therefore,

 $E_A = 4.44 f N_A \varnothing_{max} = 4.44 f N_A B_m A$

Similarly, r.m.s value of induced e.m.f in secondary is $E_B = 4.44 f N_B Ø_{max} = 4.44 f N_B B_m A$

In an ideal transformer on no load,

 $V_A = E_A$ and $V_B = E_B$, where V_B is the terminal voltage

Voltage Transformation Ratio (K) From the above equations we get $E_B/E_A = V_B/V_A = N_B/N_A = K$

This constant K is known as voltage transformation ratio.

- (1) If $N_B > N_A$, that is K>1, then transformer is called step-up transformer.
- (2) If $N_B < 1$, that is K<1, then transformer is known as step-down transformer.

Again for an ideal transformer, Input V_A = output V_A

 $V_A I_A = V_B I_B$

Or,
$$I_B/I_A = V_A/V_B = 1/K$$

Hence, currents are in the inverse ratio of the (voltage) transformation ratio.

Applications of a transformer

Transformers are used in most electronic circuits. A transformer has only 3 applications;

- 1. To step up voltage and current.
- 2. To Step down voltage and current

3. To prevent DC – transformers can pass only Alternating Currents so they totally prevent DC from passing to the next circuit.

