

LINEAR PROBING

- Probing is the process of getting next available hash table array cell.
- In linear probing, $F(i)$ is a linear function of i . That means alternative locations are searched in a sequential manner. Thus,

$$F(i)=i$$

Example:

Insert the keys {89, 18, 49, 58, 69} into the hash table.

	Empty Table	After 89	After 18	After 49	After 58	After 69
0				49	49	49
1					58	58
2						69
3						
4						
5						
6						
7						
8			18	18	18	18
9		89	89	89	89	89

$$h_i(X) = (\text{Hash}(X) + F(i)) \bmod \text{Table size}$$

$$\text{Hash}(89) = 89 \bmod 10 = 9 \text{ (No collision)}$$

$$\text{Hash}(18) = 18 \bmod 10 = 8 \text{ (No collision)}$$

Hash (49) = 49 mod 10 = 9 (Collision Occurred)

$$\begin{aligned} h_i(49) &= (\text{Hash}(49) + F(1)) \bmod 10 \\ &= (9 + 1) \bmod 10 = 10 \bmod 10 = 0 \text{(No collision)} \end{aligned}$$

Hash (58) = 58 mod 10 = 8 (Collision occurred)

$$\begin{aligned} h_i(58) &= (\text{Hash}(58) + F(1)) \bmod 10 \\ &= (8 + 1) \bmod 10 = 9 \bmod 10 = 9 \text{(Collision occurred)} \end{aligned}$$

$$\begin{aligned} h_i(58) &= (\text{Hash}(58) + F(2)) \bmod 10 \\ &= (8 + 2) \bmod 10 = 10 \bmod 10 = 0 \text{(Collision occurred)} \end{aligned}$$

$$\begin{aligned} h_i(58) &= (\text{Hash}(58) + F(3)) \bmod 10 \\ &= (8 + 3) \bmod 10 = 11 \bmod 10 = 1 \text{(No Collision)} \end{aligned}$$

Hash (69) = 69 mod 10 = 9 (Collision Occurred)

$$\begin{aligned} h_i(69) &= (\text{Hash}(69) + F(1)) \bmod 10 \\ &= (9 + 1) \bmod 10 = 10 \bmod 10 = 0 \text{(Collision occurred)} \end{aligned}$$

$$\begin{aligned} h_i(69) &= (\text{Hash}(69) + F(2)) \bmod 10 \\ &= (9 + 2) \bmod 10 = 11 \bmod 10 = 1 \text{(Collision occurred)} \end{aligned}$$

$$\begin{aligned} h_i(69) &= (\text{Hash}(69) + F(3)) \bmod 10 \\ &= (9 + 3) \bmod 10 = 12 \bmod 10 = 2 \text{(No Collision)} \end{aligned}$$

