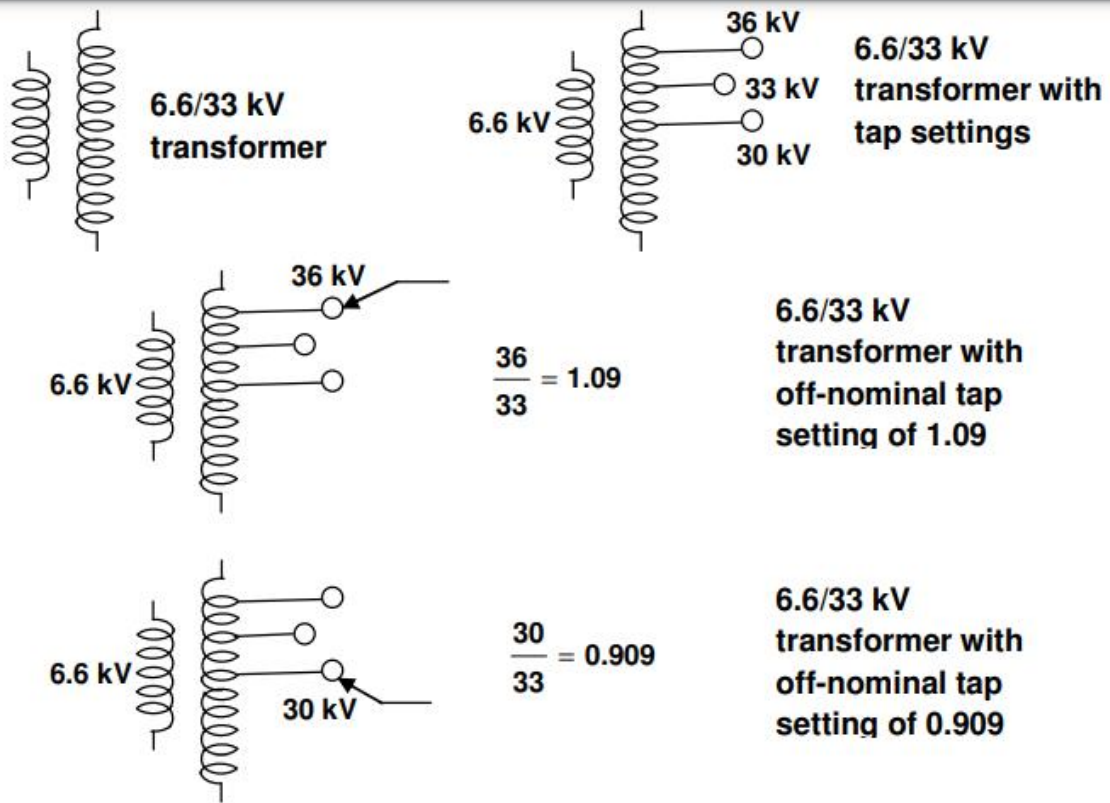
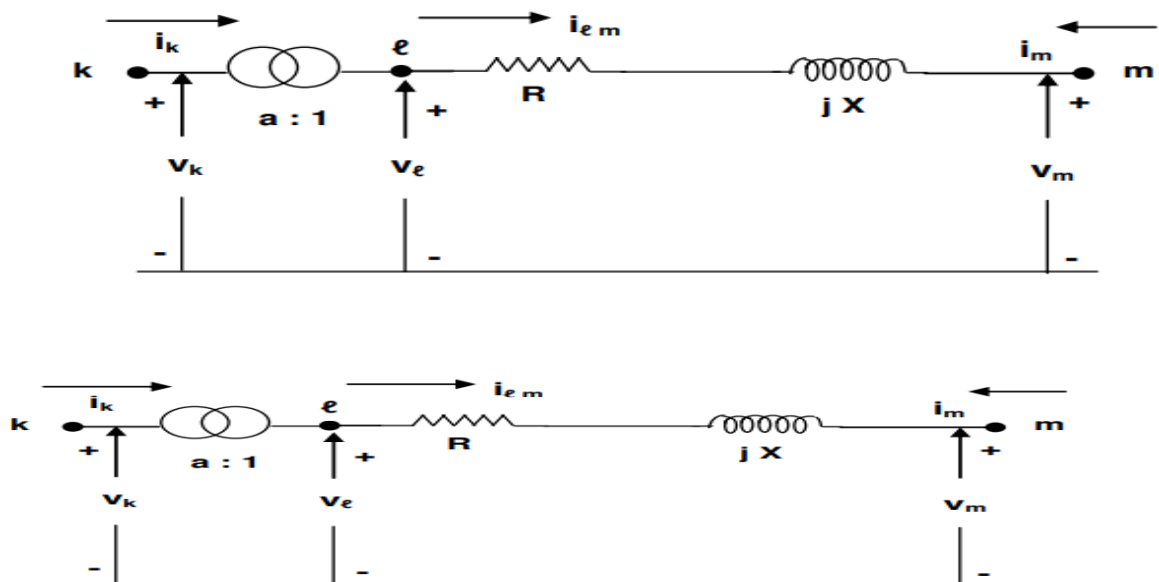


REPRESENTATION OF OFF-NOMINAL TAP SETTING TRANSFORMER



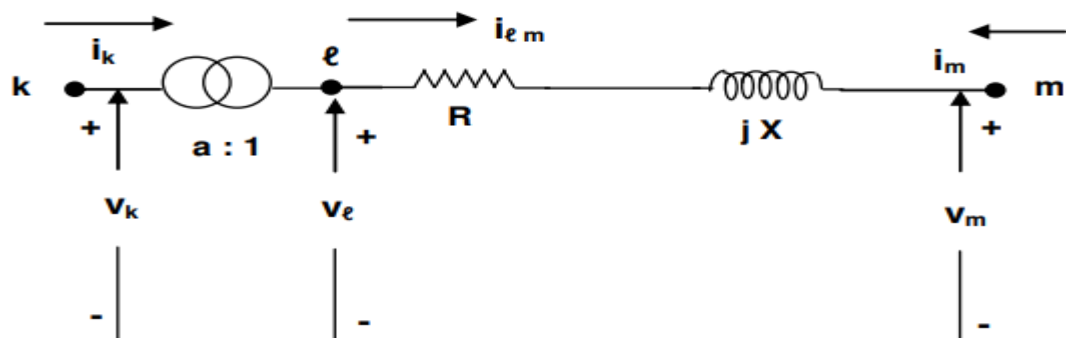
Transformers with off-nominal tap settings can be modelled as the series combination of auto-transformer with transformer impedance as shown in Figure. The two transformer terminals k and m are commonly designated as the tap side and impedance side bus respectively.

Equivalent circuit for an off-nominal tap setting transformer



The nodal equations of the two port circuit of Fig. can be derived by first expressing the current flows i_{em} and i_m at each end of the series branch $R + jX$ in terms of the terminal voltages v_l and v_m . Denoting the admittance of this branch $-m$ by y , the terminal current injection will be given by

$$\begin{bmatrix} i_{em} \\ i_m \end{bmatrix} = \begin{bmatrix} y & -y \\ -y & y \end{bmatrix} \begin{bmatrix} v_l \\ v_m \end{bmatrix}$$



$$\begin{bmatrix} i_{em} \\ i_m \end{bmatrix} = \begin{bmatrix} y & -y \\ -y & y \end{bmatrix} \begin{bmatrix} v_e \\ v_m \end{bmatrix}$$

Knowing that $v_k / v_e = a$ and $i_m / i_k = a$, substituting for i_m and v_l as

$$i_{em} = a i_k; \quad v_e = v_k / a \quad \text{we get} \quad \begin{bmatrix} a i_k \\ i_m \end{bmatrix} = \begin{bmatrix} y & -y \\ -y & y \end{bmatrix} \begin{bmatrix} v_k/a \\ v_m \end{bmatrix}$$

The final form will be obtained as

$$\begin{bmatrix} i_{em} \\ i_m \end{bmatrix} = \begin{bmatrix} y & -y \\ -y & y \end{bmatrix} \begin{bmatrix} v_e \\ v_m \end{bmatrix}$$

Knowing that $v_k / v_e = a$ and $i_m / i_k = a$, substituting for i_m and v as

$$i_{em} = a i_k; \quad v_e = v_k / a \quad \text{we get} \quad \begin{bmatrix} a i_k \\ i_m \end{bmatrix} = \begin{bmatrix} y & -y \\ -y & y \end{bmatrix} \begin{bmatrix} v_k/a \\ v_m \end{bmatrix}$$

The final form will be obtained as

$$\begin{bmatrix} i_k \\ i_m \end{bmatrix} = \begin{bmatrix} \frac{y}{a^2} & -\frac{y}{a} \\ -\frac{y}{a} & y \end{bmatrix} \begin{bmatrix} v_k \\ v_m \end{bmatrix}$$